## **PSC 2024**

The Praga Stringology Conference

Prague Czech Republic August 26-27, 2024





# Beyond Horspool: A Comparative Analysis in Sampled Matching

Simone Faro<sup>1</sup>, Francesco Pio Marino<sup>1,2</sup>, Andrea Moschetto<sup>1</sup>

Dipartimento di Matematica e Informatica, Università di Catania, viale A.Doria n.6, 95125, Catania, Italia

<sup>2</sup> Univ Rouen Normandie, INSA Rouen Normandie, Université Le Havre Normandie, Normandie Univ, LITIS UR 4108, CNRS NormaSTIC FR 3638, IRIB, Rouen F-76000, France

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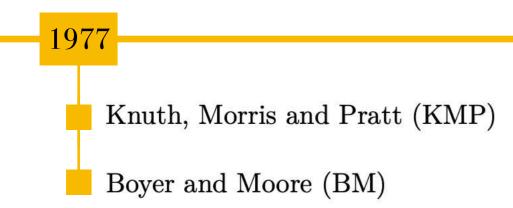
**Abstract.** The exact online string matching problem, pivotal in fields ranging from computational biology to data compression, involves identifying all instances of a specified pattern within a text. Despite extensive examination over the decades, this problem has remained computationally challenging due to the time and space limitations inherent in traditional online and offline methods, respectively. Introduced in 1991, sampled string matching has now emerged as a groundbreaking approach, ingeniously combining classical online string matching techniques with efficient text sampling methods. This approach not only addresses the spatial constraints of indexed string matching but also significantly reduces the search duration in online environments, achieving speed increases of up to hundreds of times while requiring less than 4% of the text size for its partial index. In this paper, we explore the adaptability of various online string matching algorithms within the framework of sampled string matching, which has traditionally relied on the Horspool algorithm. Our investigation reveals that integrating alternative string matching algorithms as subroutines markedly enhances overall performance. These findings highlight the potential for reevaluating established methodologies in light of newer, more dynamic solutions and set the stage for transformative impacts across multiple domains.

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# Online and Offline String Matching

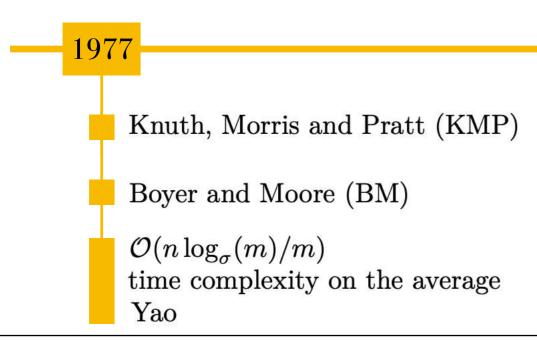
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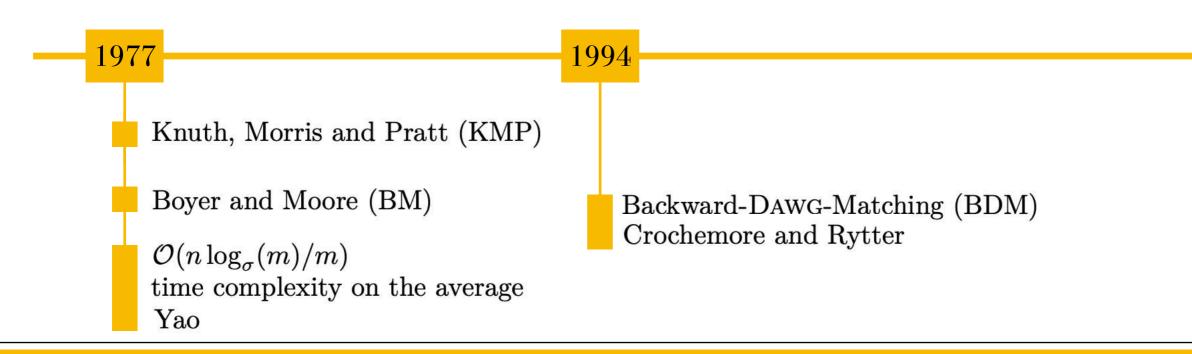
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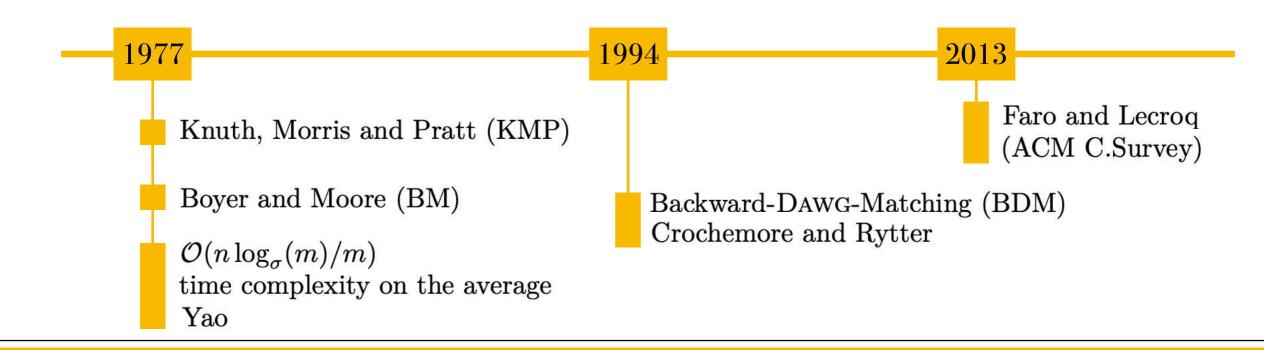
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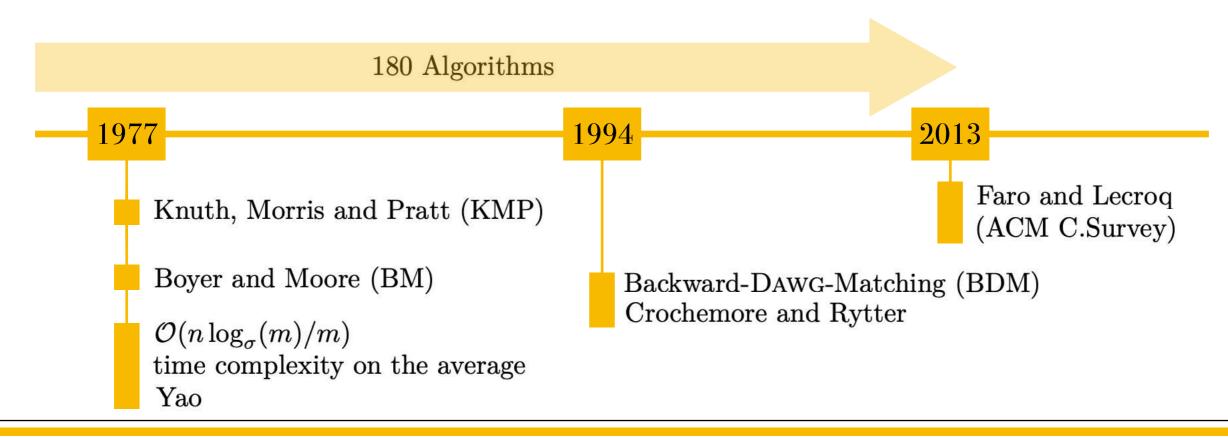
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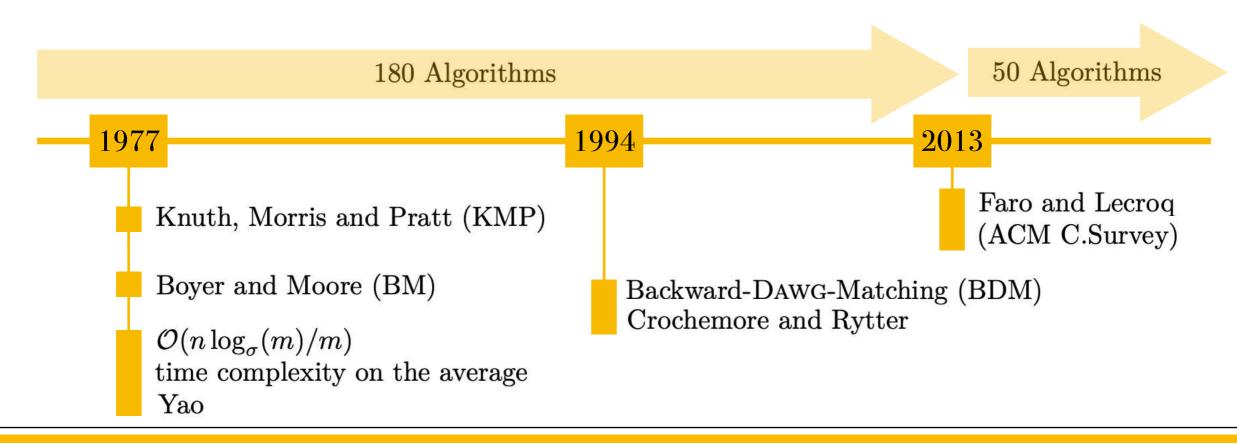
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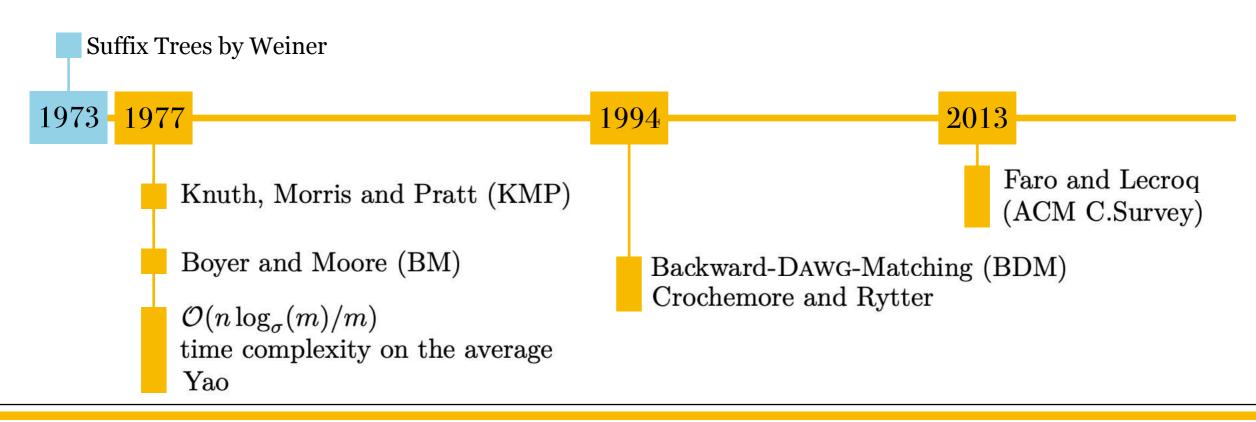
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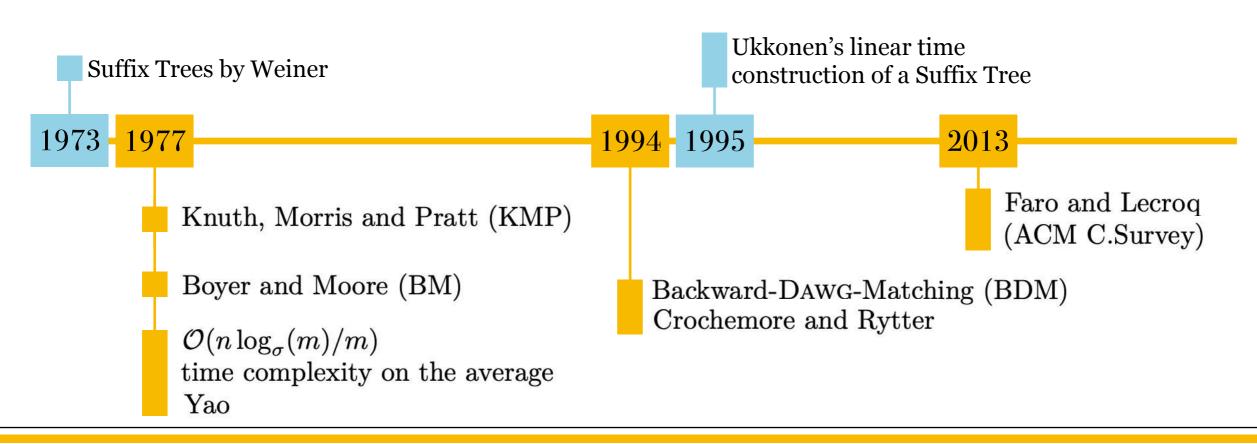
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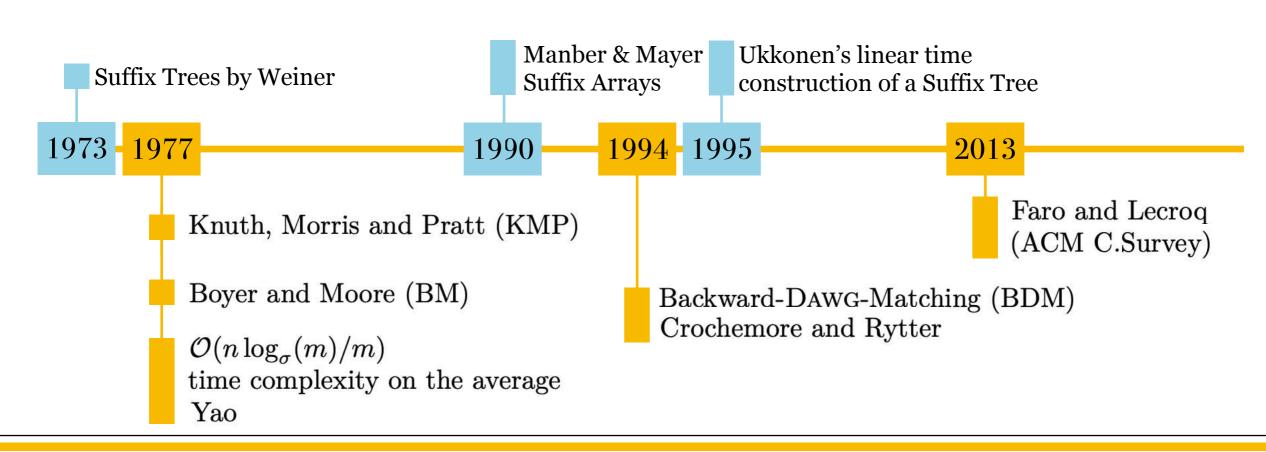
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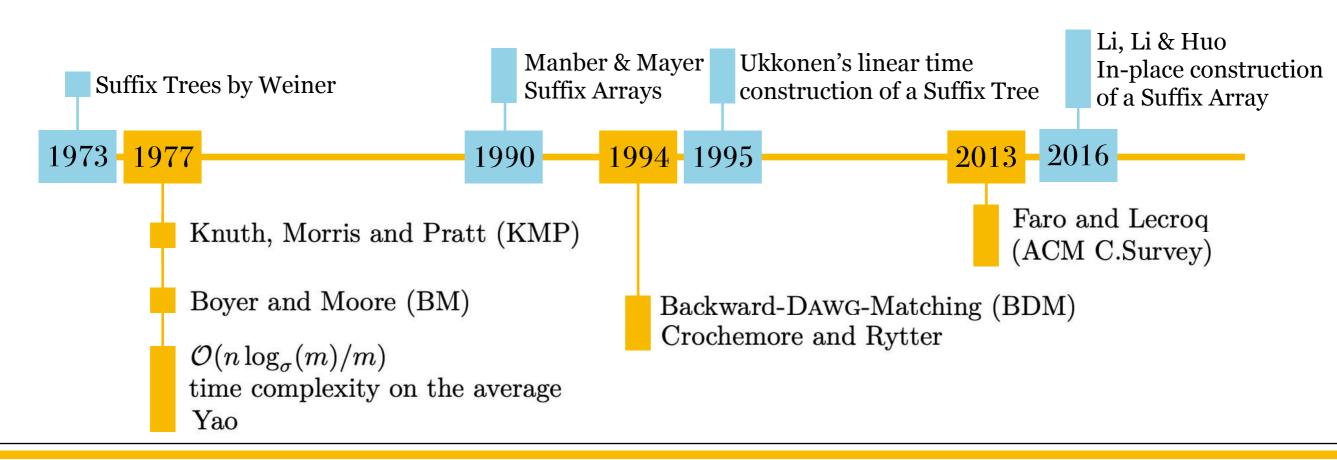
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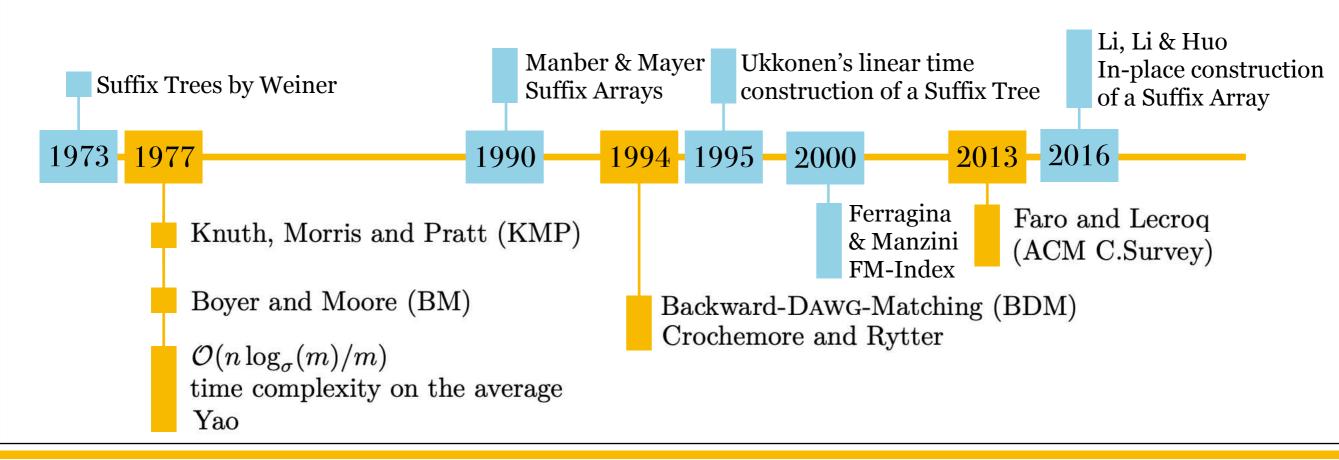
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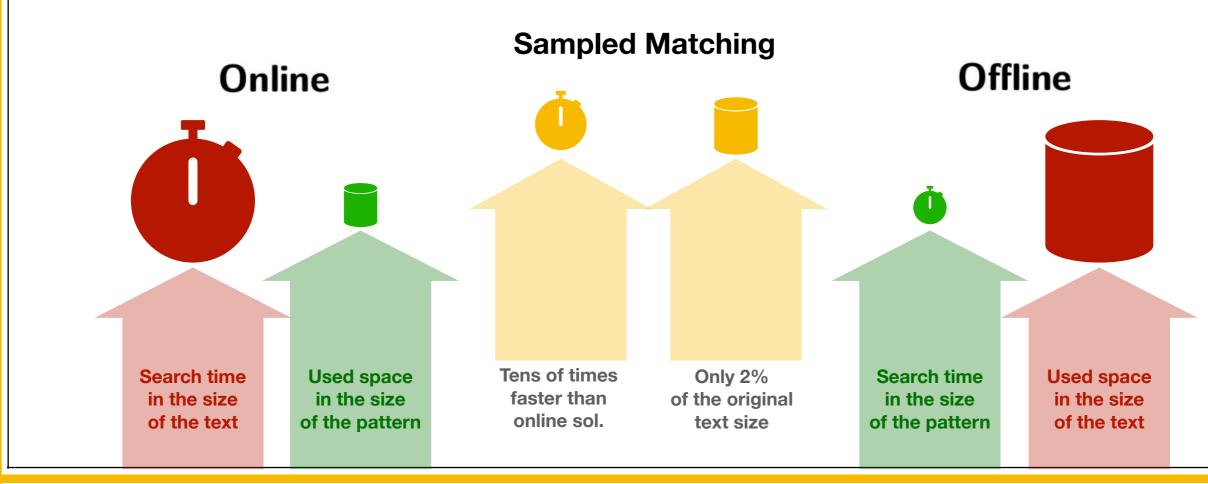
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#### Online and Offline String Matching



Sampled String Matching involves creating a succinct version of the text and then applying online string matching algorithms directly to the new version. This technique enables faster discovery of pattern occurrences, but each discovery within the sampled version of the text requires subsequent verification within the original text.

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- it typically necessitates straightforward implementation
- it demands only a limited amount of additional space
- it enables fast search and update operations



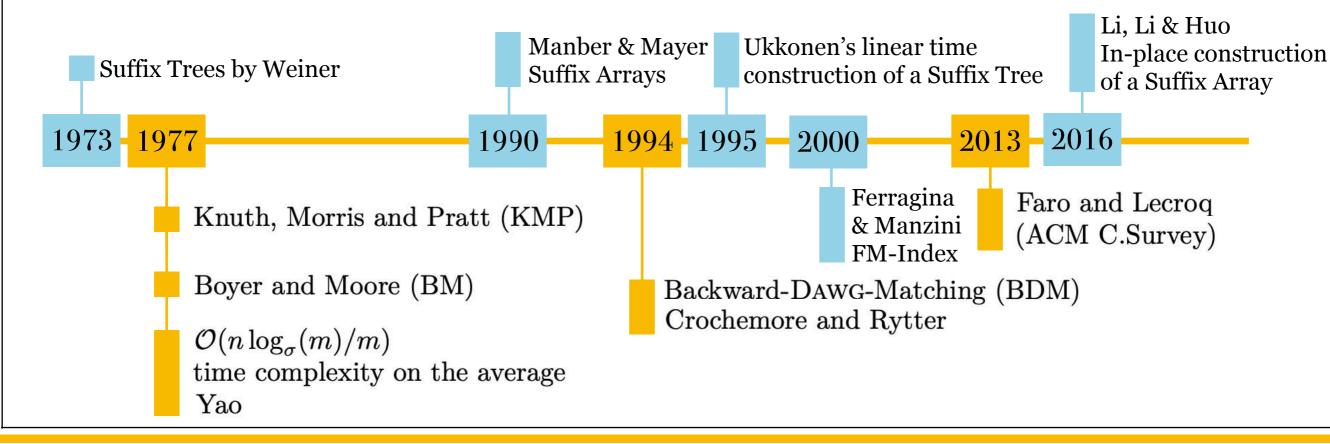
Easy to implement



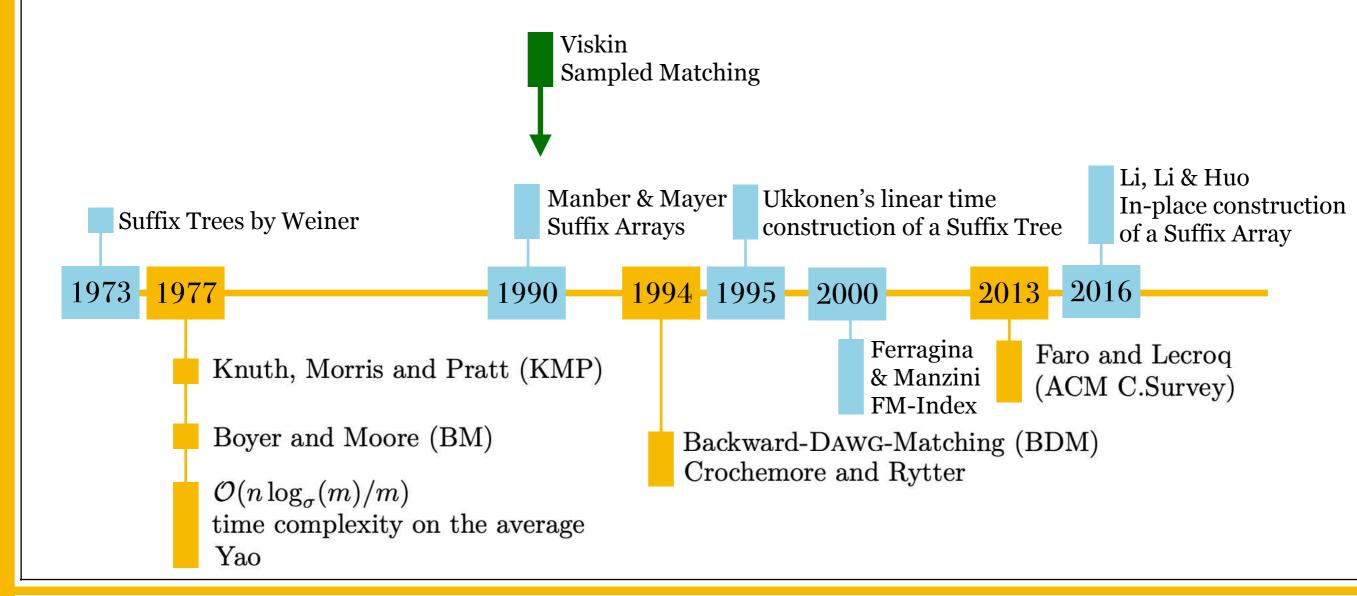
Limited space

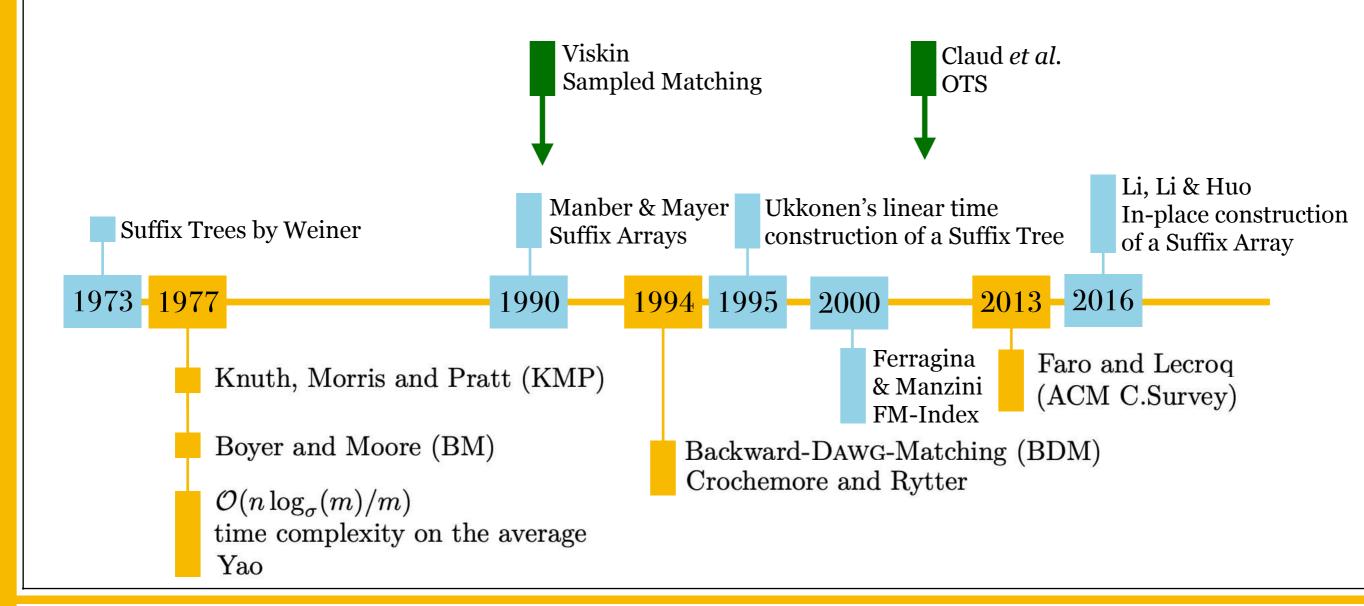


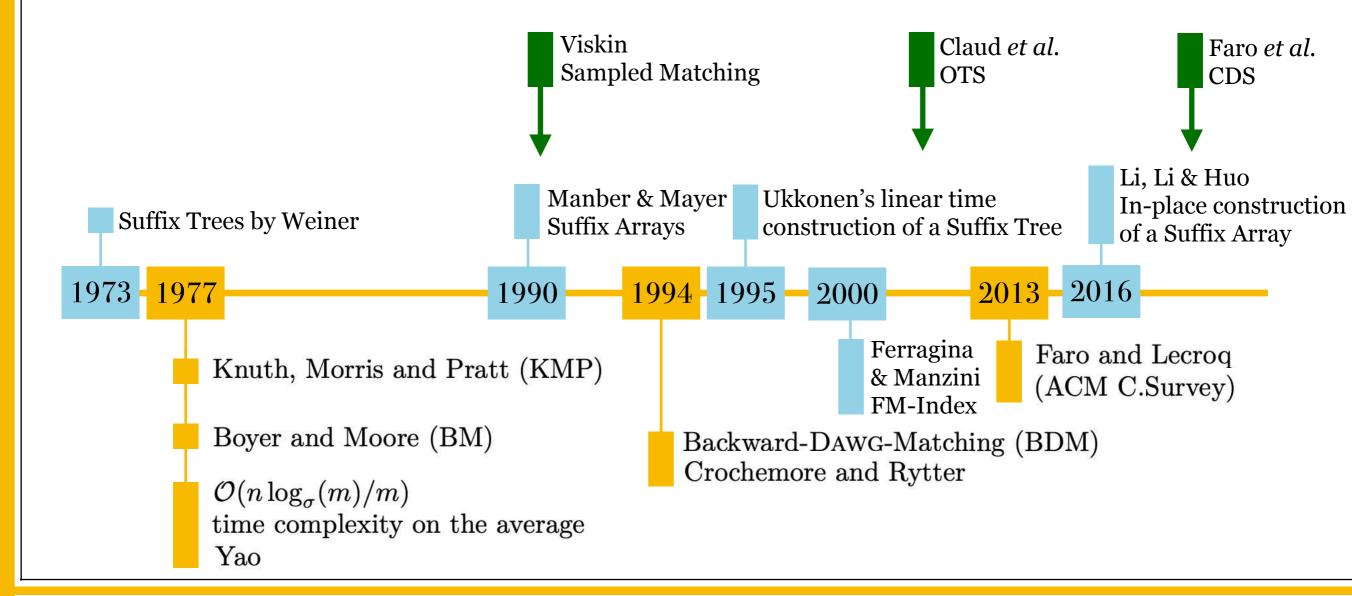
Very fast operations













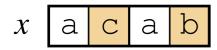
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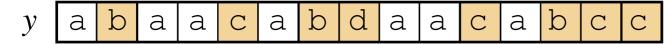
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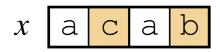


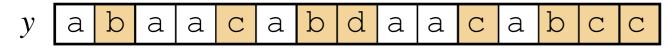


$$\Sigma = \{a,b,c,d\}$$

$$\hat{x}$$
 cb

$$\hat{\Sigma} = \{ b, c, d \}$$

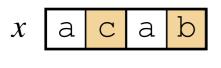


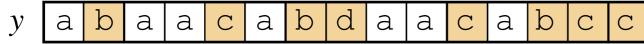


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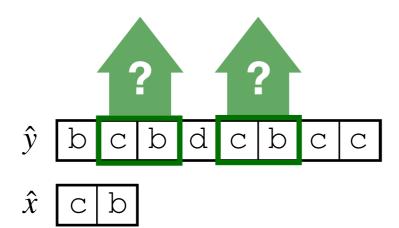
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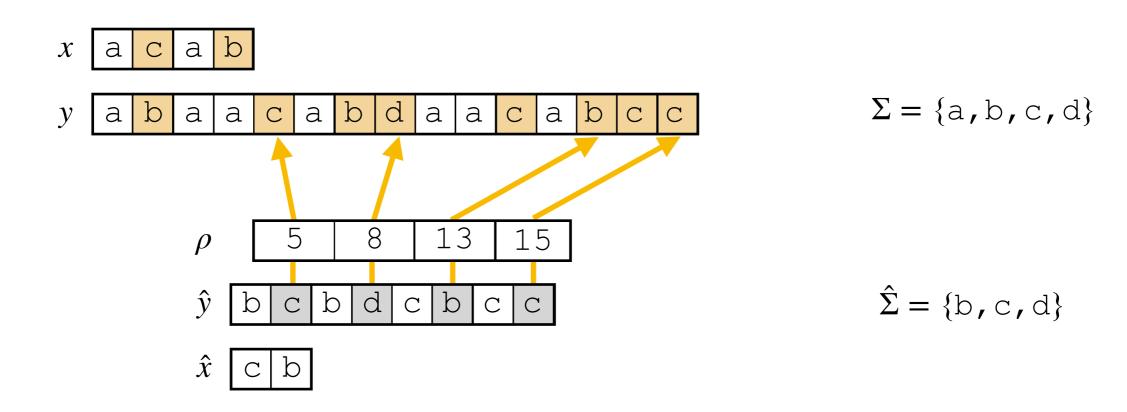


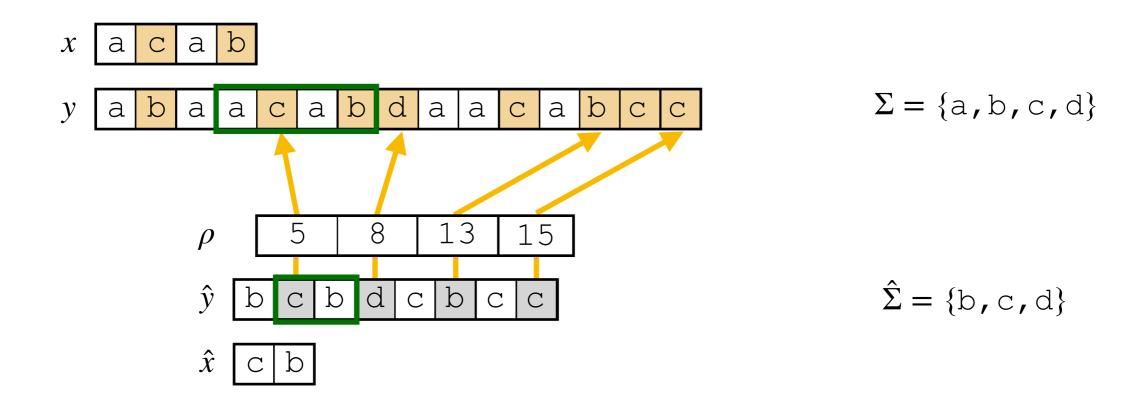


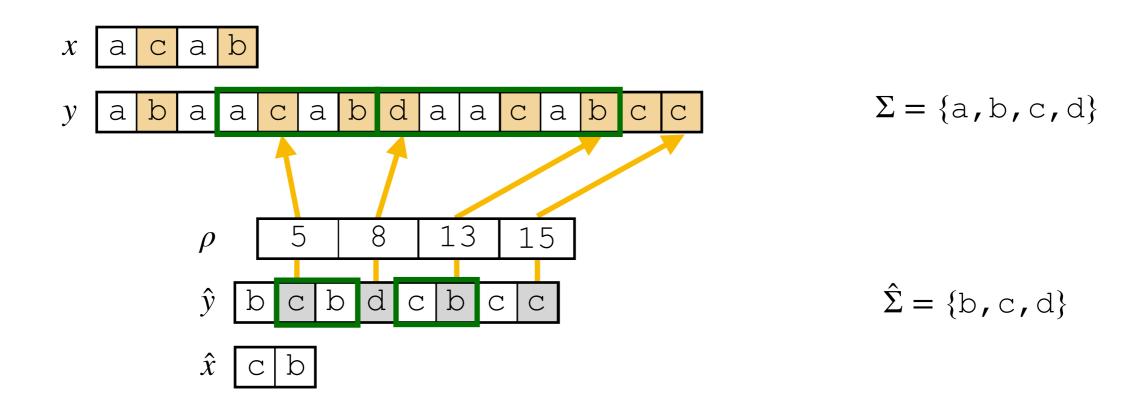
$$\Sigma = \{a,b,c,d\}$$



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5 times faster



14% of the text size

# **CDS: Character Distance Text-Sampling**

CDS selects a sub-alphabet  $C \subseteq \Sigma$  to serve as the set of pivot characters. Using these designated pivots, it is possible to sample the text y by calculating the distances between the  $n_c$  consecutive occurrences of any pivot character  $c \in C$  within y. Formally, this sampling methodology is based on the definition of position sampling within a text. Given  $\delta: \{1, ..., n_c\} \to \{1, ..., n\}$ , where  $\delta(i)$  is the position of the i-th occurrence of any pivot character c in y. Then the position sampled version of y, indicated by  $\dot{y}$ , is a numeric sequence, of length  $n_c$ , defined as  $\dot{y} = \langle \delta(1), \delta(2), ..., \delta(n_c) \rangle$ .

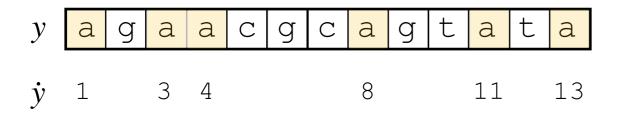
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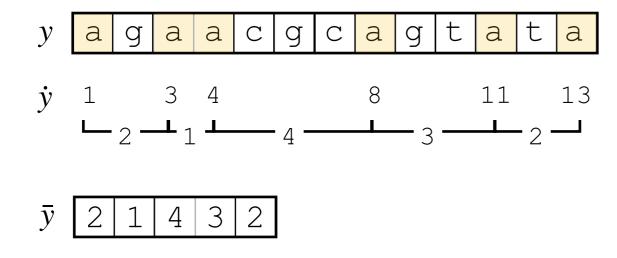


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The characters-distance sampled version of the text y is a numeric sequence, indicated by  $\bar{y}$ , of length  $n_c - 1$  defined as  $\bar{y} = \langle \delta(2) - \delta(1), \delta(3) - \delta(2), ..., \delta(n_c) - \delta(n_c - 1) \rangle$ 

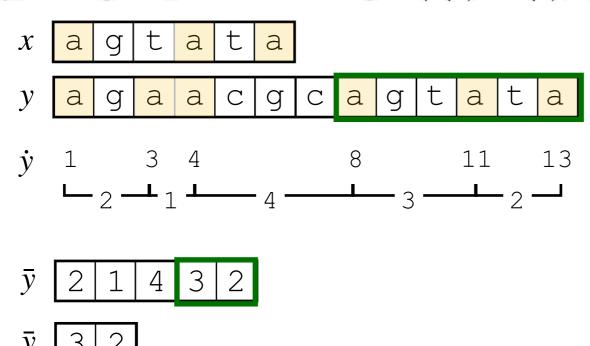


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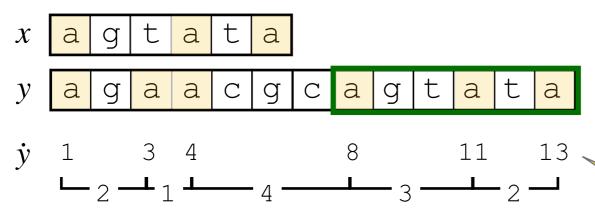


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In order to map sampled positions to real positions CDS maintains  $\dot{y}$  and compute  $\bar{y}$  on the fly



The pivot character does not occur in x, thus  $|\bar{x}| = 0$ We search for x in the white intervals, where the pivot character does not occur

y

Case o

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Case 1

The pivot character occurs only once in x, thus  $|\bar{x}| = 1$ We use the sampled text as a set of anchors to locate candidate positions in y



 $\mathcal{X}$ 

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Case 1 The pivot character occurs only once in x, thus  $|\bar{x}| = 1$  We use the sampled text as a set of anchors to locate candidate positions in y



x

Case 2 The pivot character occurs more than once in x, thus  $|\bar{x}| > 1$  We search for  $\bar{x}$  in  $\bar{y}$  and verify any candidate occurrence in the original text



 $\bar{x}$ 





9 times faster



2% of the text size

## **Experimental Results**

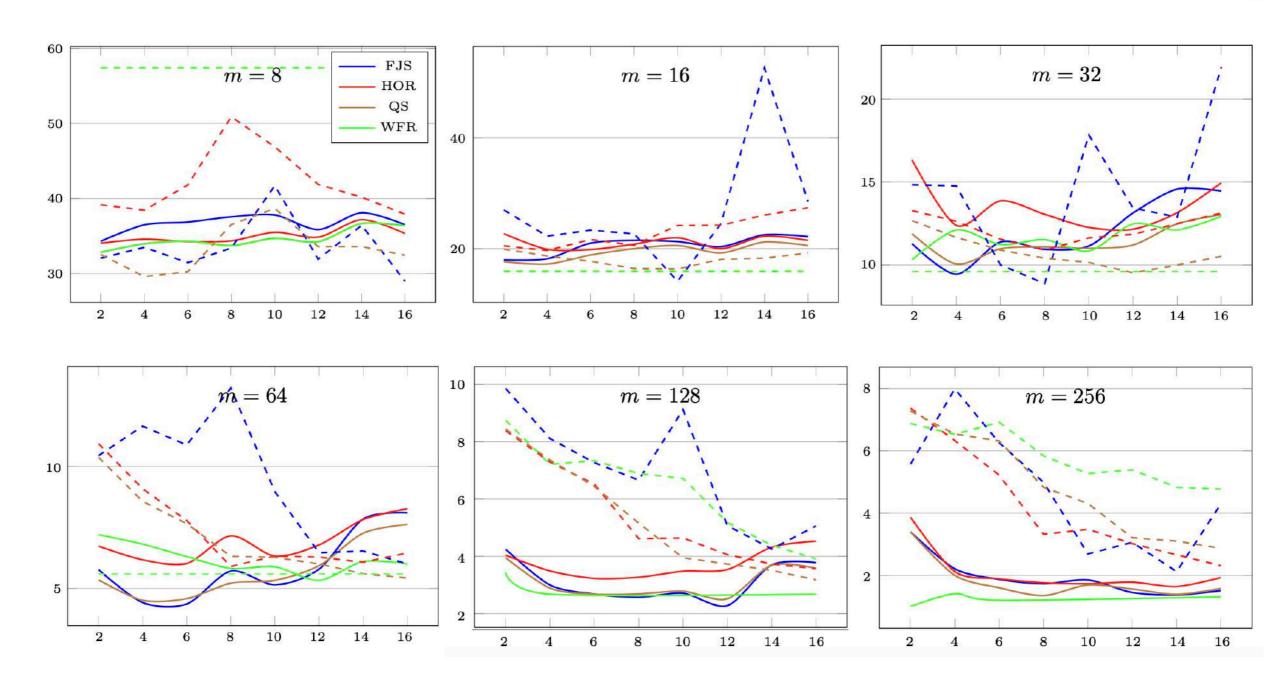
Two text buffers, each with a size of 100 MB, were used, sourced from the *Pizza and Chili* dataset [15], available online for download. Specifically, the algorithms were tested using a genomics data sequence and a natural language text. For each sequence, 500 patterns were randomly selected from the text, and the average running time was computed over the 500 runs.

We tested the OTS and CDS approach using the following algorithms:

- HOR Horspool
- QS Quick Search
- FJS Franek-Jennings-Smyth
- WFR Weak-Factor Recognition

## **Experimental Results**

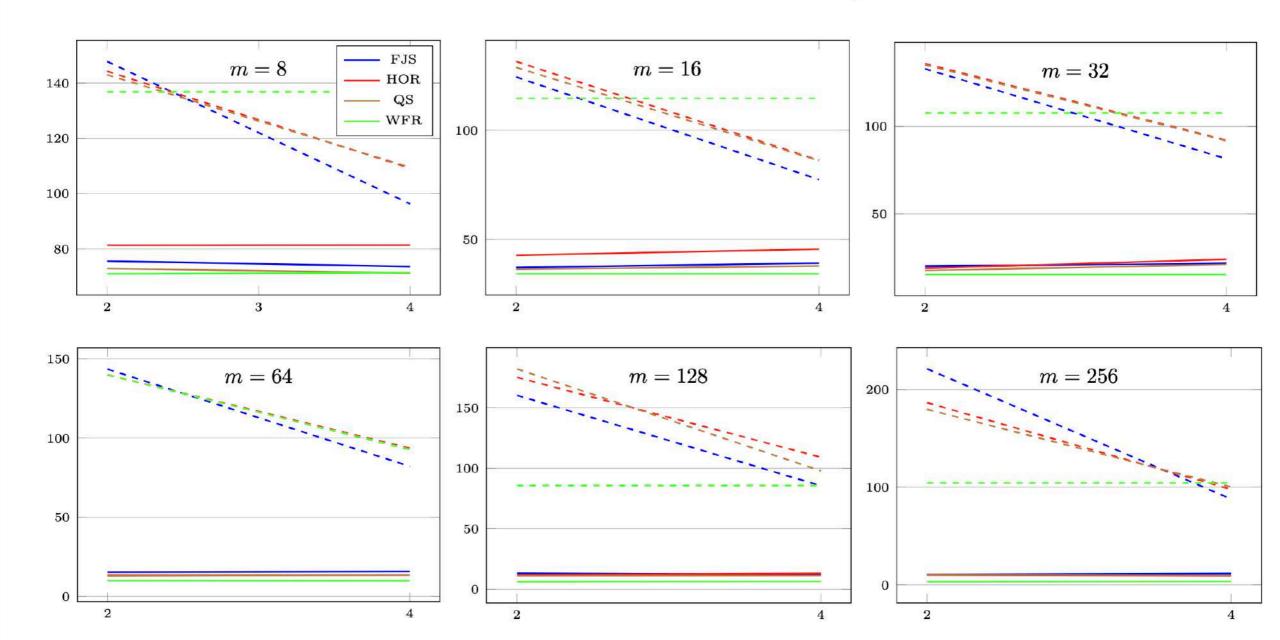
#### Online Searching on Natural Language Sequence





## **Experimental Results**

#### Online Searching on Genomics Sequence





#### Conclusions

In this paper we have presented an extension of the text sampling approaches, called Character Distance and Occurrence Text Sampling, to the case of applying different searching algorithms. This extension was carried out using four different well known algorithms. Our results proved the efficacy of the sampled methods discussed in this paper and their versatility to be adapted to any online string matching algorithms without impacting their original performances.

Although our tests were limited to the exact string matching problem, obtaining excellent results, we believe that the approach can be effectively generalized even to non-standard string matching. Our future studies will focus in this direction in order to apply sampled string matching to other problems related to text processing.

Thanks

