

# Taxonomies of Regular Tree Algorithms

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Technische Universiteit  
**Eindhoven**  
University of Technology

Where innovation starts

PSC 2009, Prague, September 2<sup>nd</sup> 2009

- **Context**  
*History & relevance, deficiencies, role of taxonomies & toolkits*
- **Domain**  
*Trees, patterns & matching, regular tree grammars*
- **Taxonomies**  
*Algorithm taxonomies, taxonomies of regular tree algorithms*
- **Tree Acceptance Taxonomy**  
*Algorithms b/o tree automata, match sets, stringpath matching*
- **Concluding Remarks**

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  - *Membership/Tree Acceptance*
  - *Tree Pattern Matching*
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  - Construct and use *TA* based on *RTG* or pattern set

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- **1960s**
  - Equivalence between formalisms (except Deterministic Top-Down/Root-to-Frontier TA), transformations between them
  - Construct and use *TA* based on *RTG* or pattern set
- **Since ca. 1975**
  - Applications in instruction selection, term rewriting, model checking
  - Many *TA* constructions, algorithms

# Context

## Appearance of algorithms

- *Brainerd, 1967 & 1969*
- *Kron, 1975*
- *Hoffmann & O'Donnell, 1980 & 1982*
- *Hatcher, 1985; Hatcher & Christopher, 1986*
- *Turner, 1986*
- *van Dinther, 1987*
- *Chase, 1987*
- *Aho, Ganapathi & Tjang, 1985, 1988*
- *van de Meerakker, 1988*
- *Weisgerber & Wilhelm, 1989*
- *Hemerik & Katoen, 1989*
- *Balachandran, Dhamdhere & Biswas, 1990*
- *Ferdinand, Seidl & Wilhelm, 1994*
- *Wilhelm & Mauer, 1995*
- *Comon et al., 2003*
- *Cleophas, Hemerik & Zwaan, 2005 & 2006*
- *Cleophas, 2008*



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- Domain deficiencies
  - inaccessible, difficult to find
  - difficult to compare, choose
  - separation between theory and practice

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  - well-established theory
  - algorithmic problems related, with related solutions  
*Tree Acceptance, Tree Pattern Matching (TPM), Tree Parsing*

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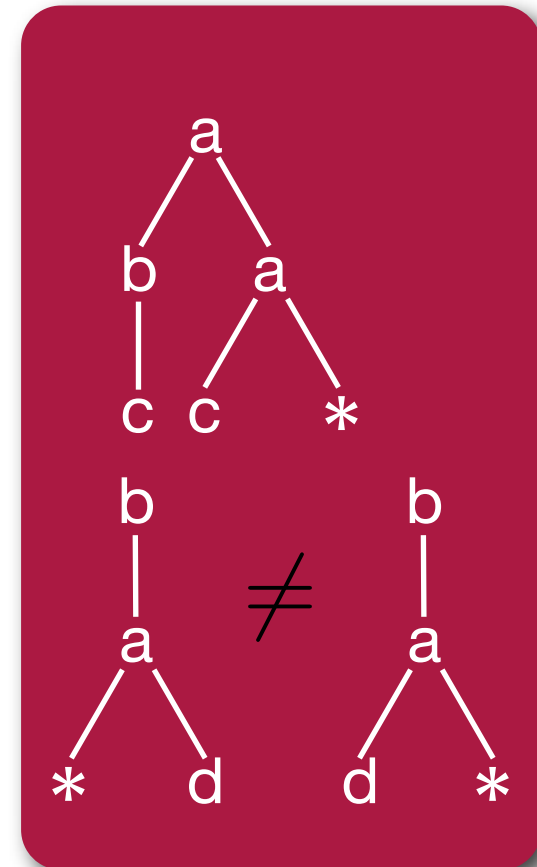
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*Tree Acceptance, Tree Pattern Matching (TPM), Tree Parsing*
- hence
  - taxonomies (*Cleophas, Hemerik & Zwaan, 2005/2006; Cleophas, 2008*)  
*systematic classifications of problems & solutions in (algorithmic) domain, to bring order to the domain*
  - toolkit (*Strolenberg, 2007; Cleophas, 2008*)  
*taxonomy-based*

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## Trees, Patterns, Tree Pattern Matching

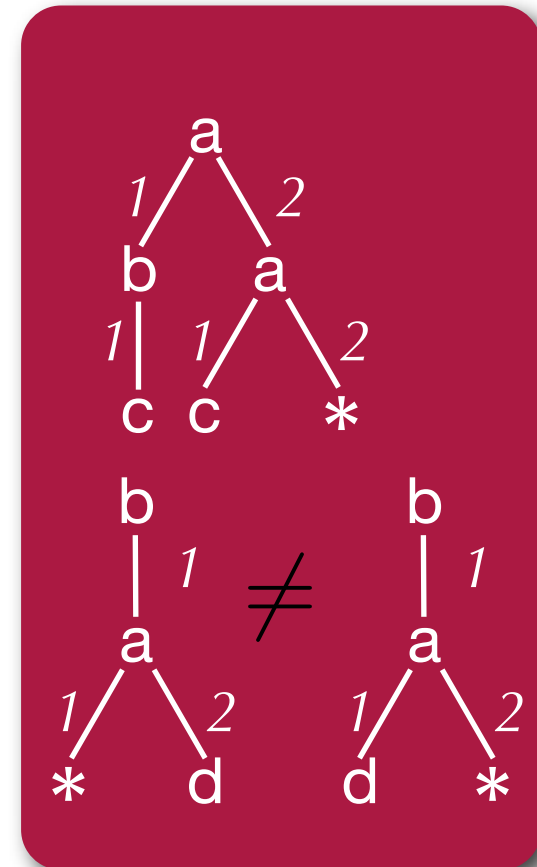
- *Node-labeled, ordered, ranked trees*
- **Generalization of strings:**  
Allow symbols of arity/rank  $\geq 1$ 
  - Fixed arity per symbol



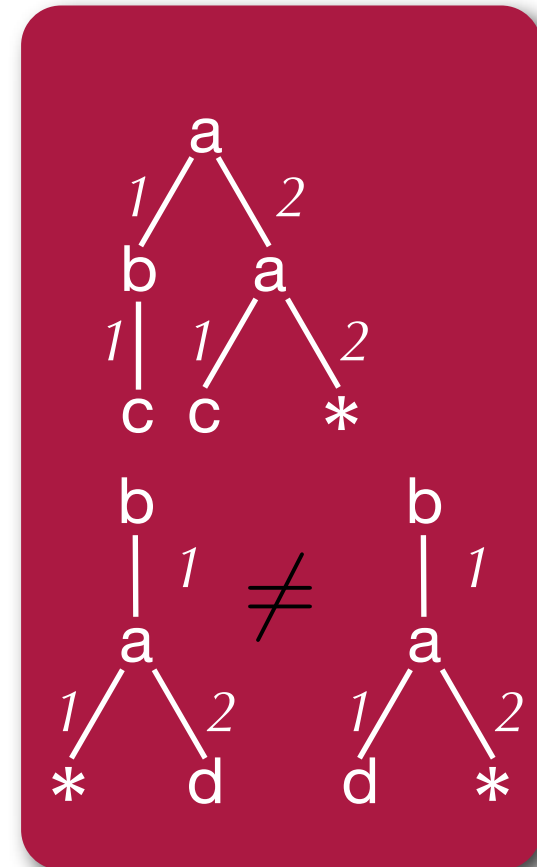
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- **Tree patterns with wildcards at leaves**





# Domain

## Regular Tree Grammars

- Generalization of regular string grammar
- Recall right regular string grammar production forms

$$A \rightarrow wB, A \rightarrow w \quad (w \in \Sigma^*)$$

# Domain

## Regular Tree Grammars

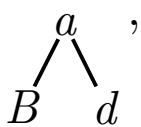
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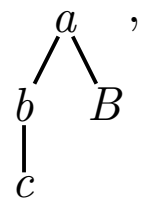
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- Regular tree grammar
  - Form  $A \rightarrow t$  with  $t$  a tree, nonterminals at leaves

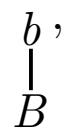
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## Regular Tree Grammars

(1)  $S \rightarrow$  ,  
 $\begin{array}{c} a \\ / \quad \backslash \\ B \quad d \end{array}$

(2)  $S \rightarrow$  ,  
 $\begin{array}{c} a \\ / \quad \backslash \\ b \quad B \\ | \\ c \end{array}$

(3)  $S \rightarrow c,$

(4)  $B \rightarrow$  ,  
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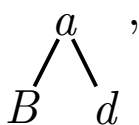
(5)  $B \rightarrow S,$

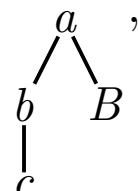
(6)  $B \rightarrow d$

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$$A \rightarrow wB, A \rightarrow w \quad (w \in \Sigma^*)$$
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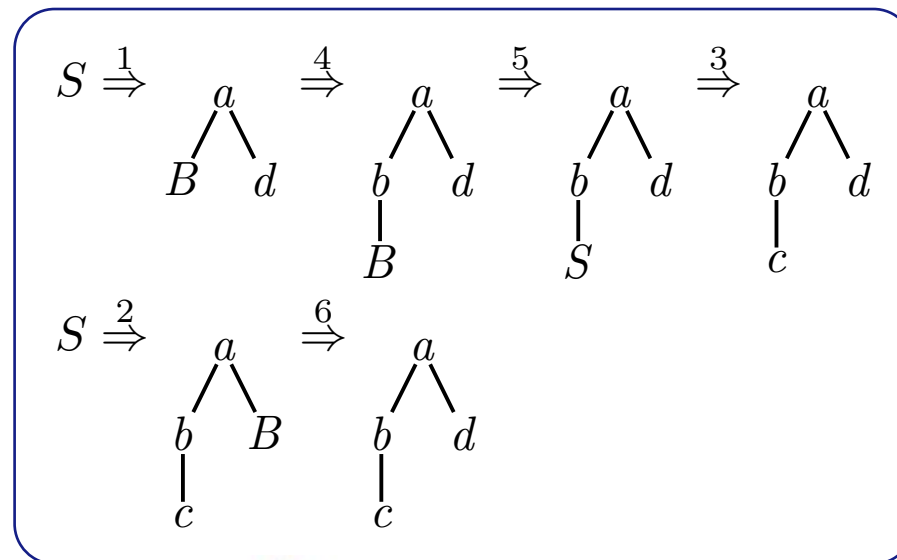
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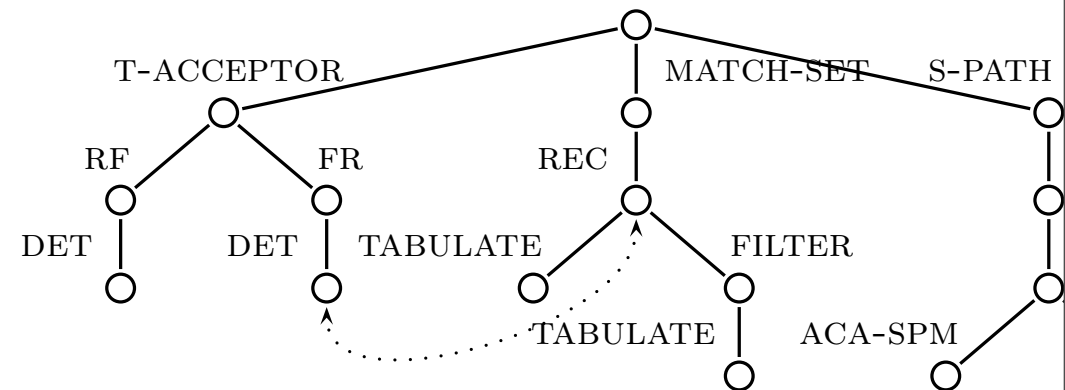


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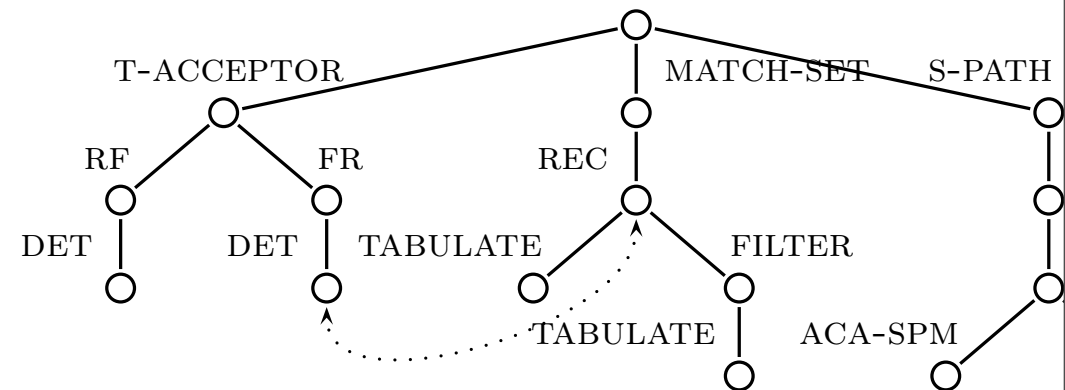
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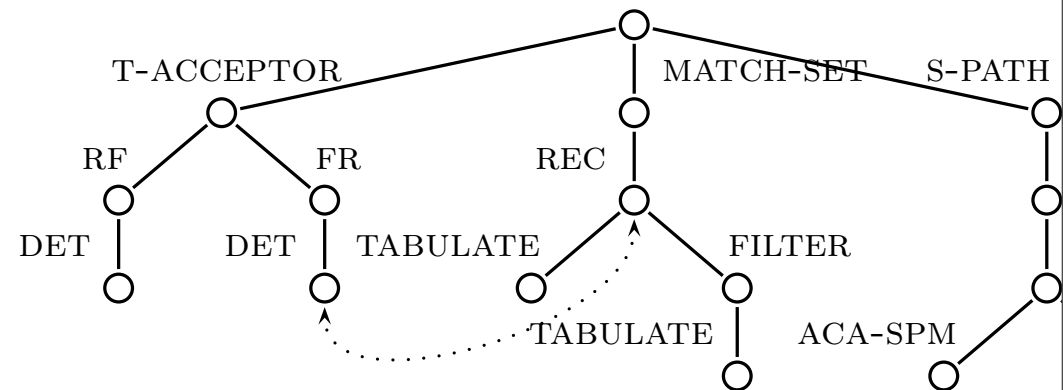
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- Depicted as tree/directed acyclic graph  
*Nodes refer to algorithms, branches to details*

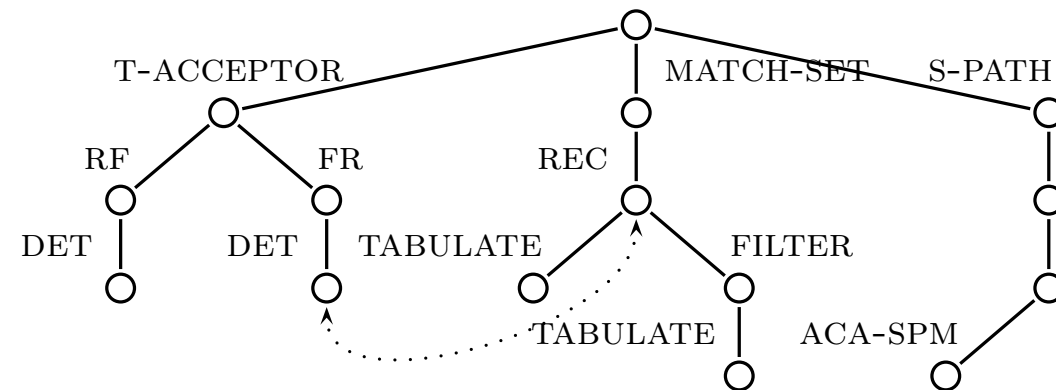




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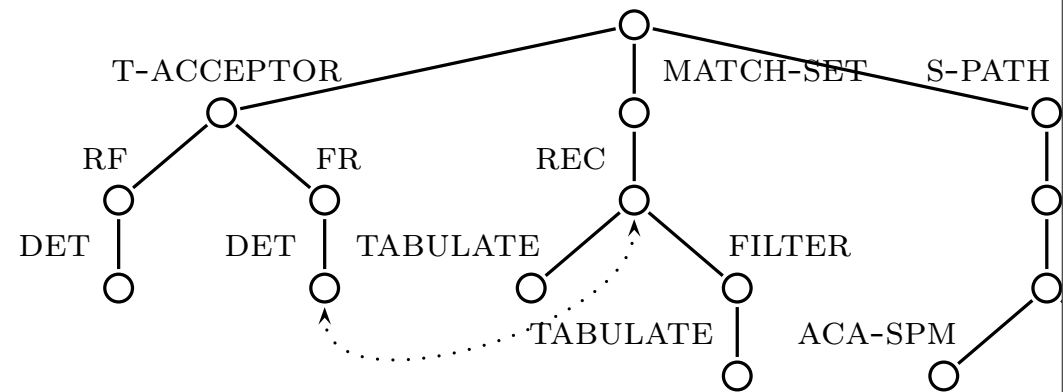
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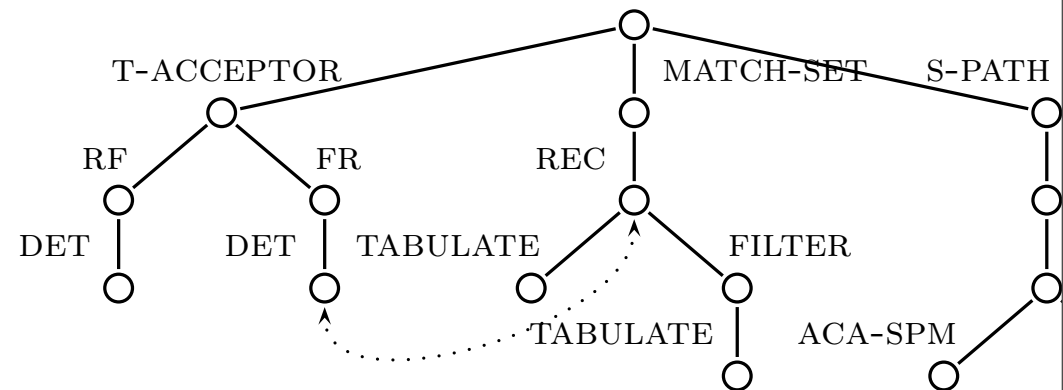
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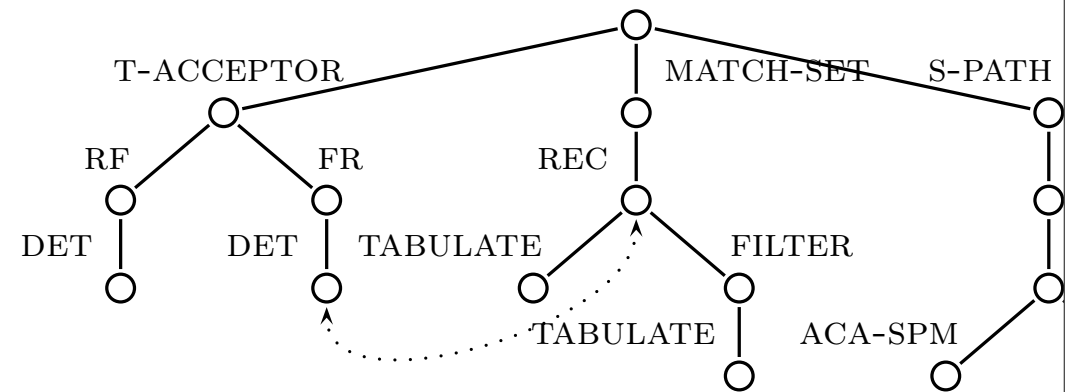
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- Properties (details) explicit
- Allow comparison, discovery of new algorithms

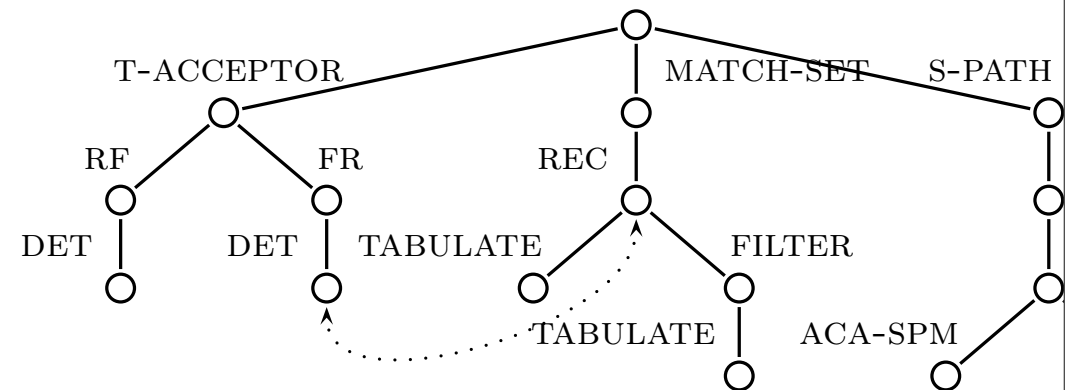


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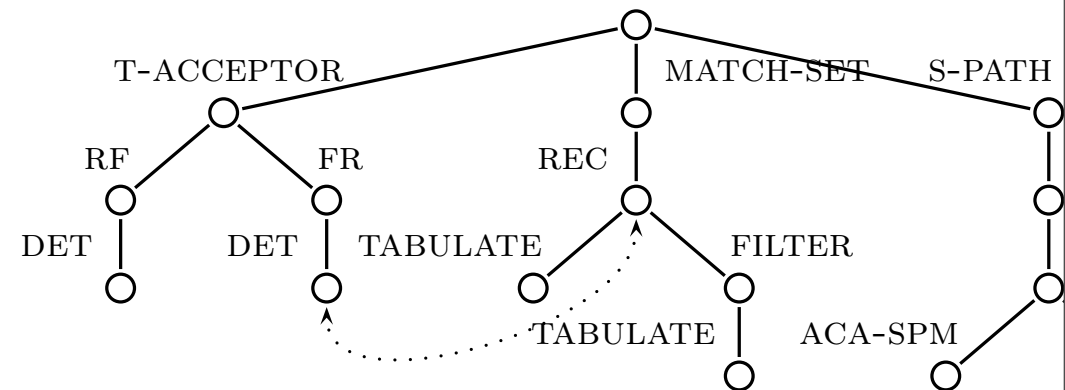
- Bottom-up





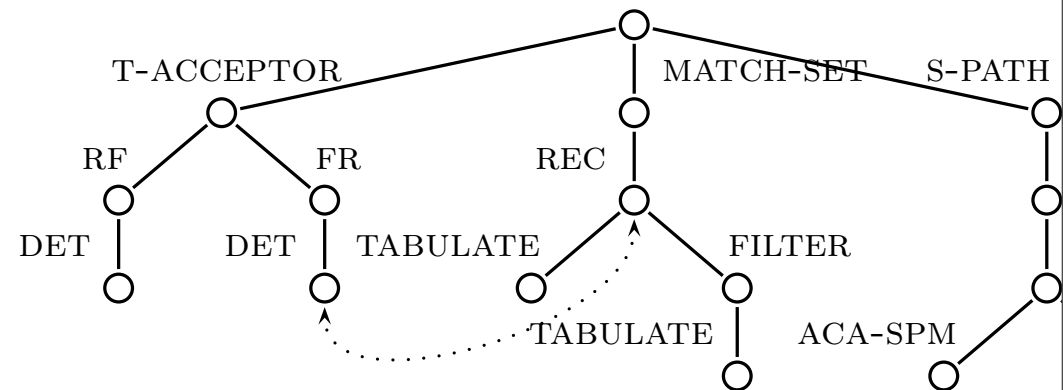
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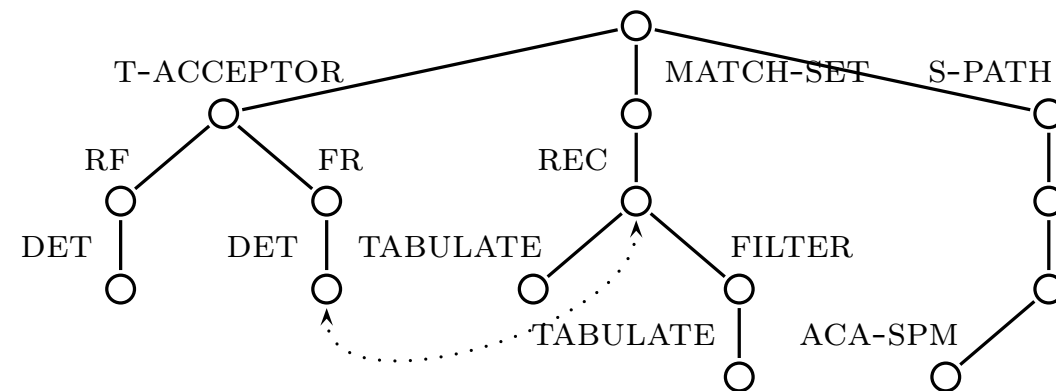
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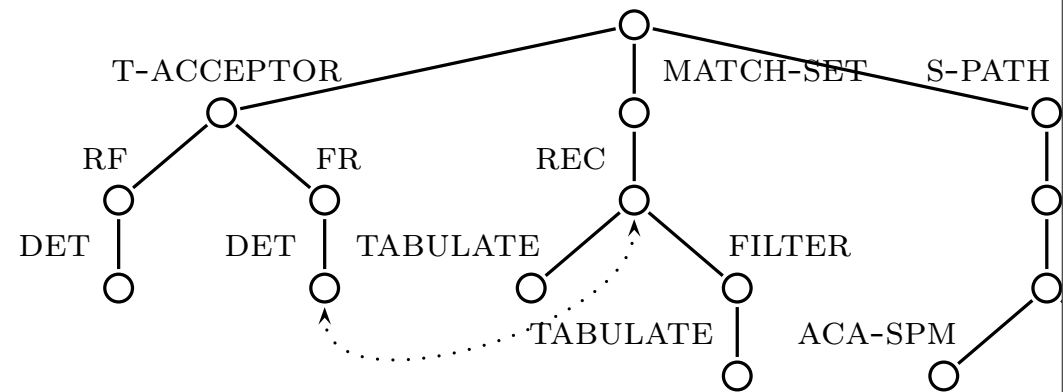
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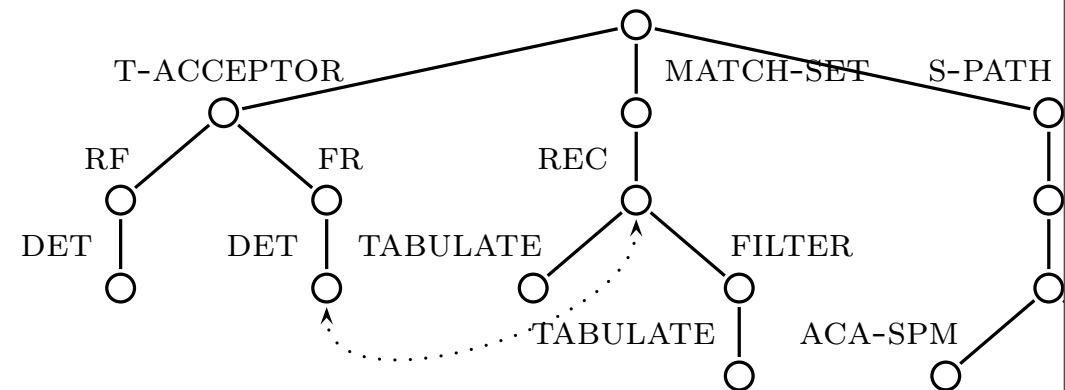
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- Abstracting over details of algorithms yields common ancestors
- New combinations may lead to new algorithms



# Taxonomies

## Presentation & Correctness

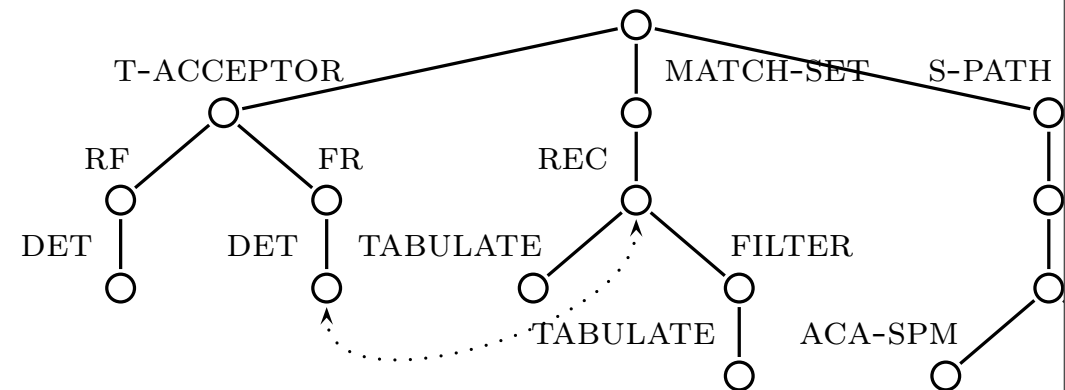
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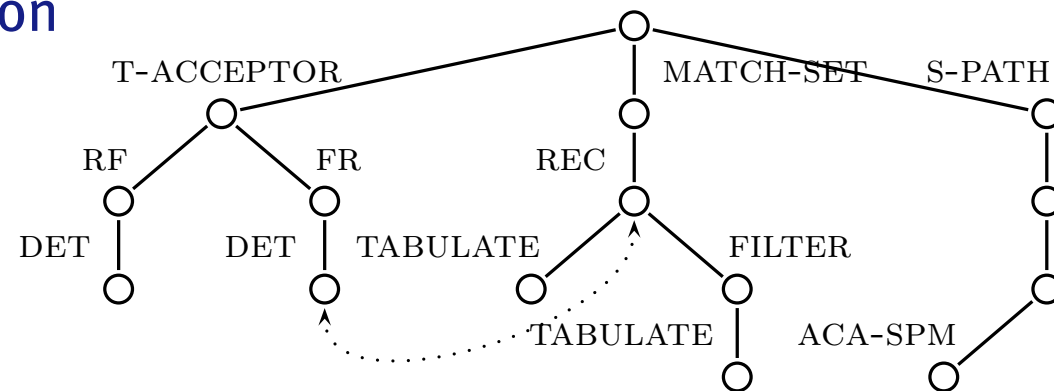
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- Root represents high-level algorithm
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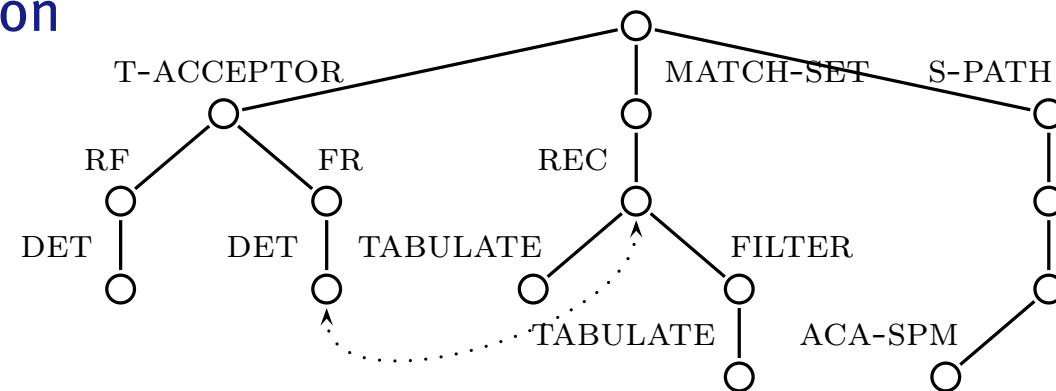
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- Adding *detail*
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  - Branch connecting algorithm node to child node
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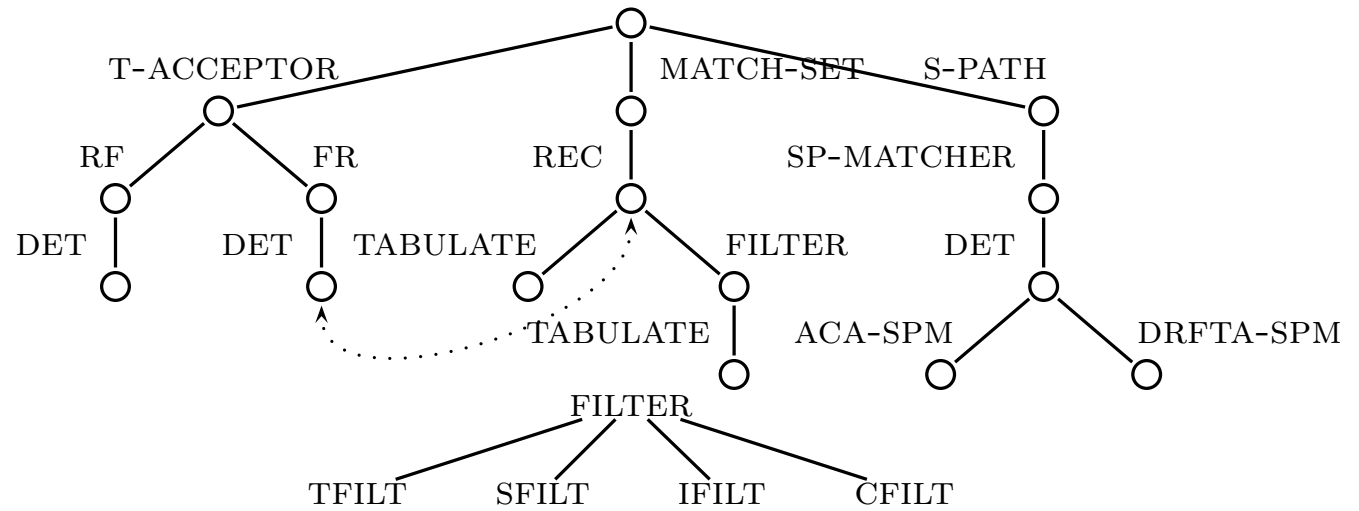
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- Correctness of root and of details on rootpath imply correctness of node



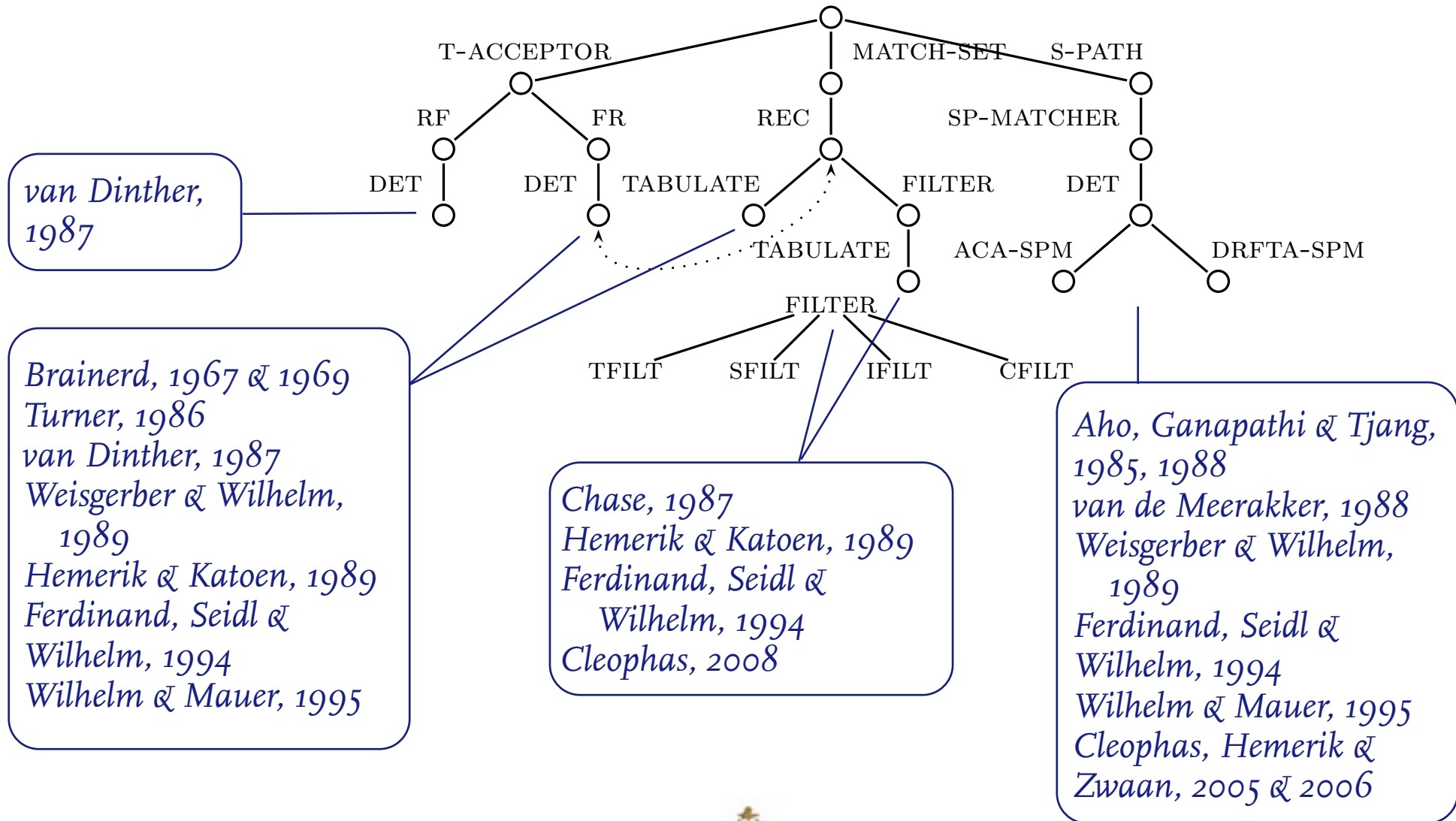
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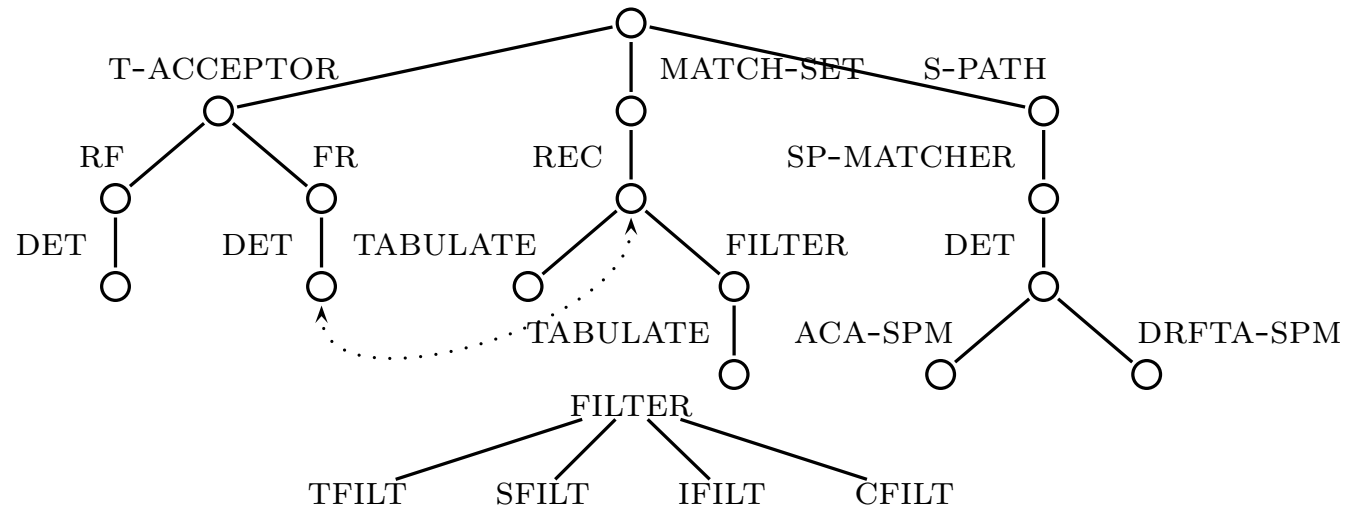




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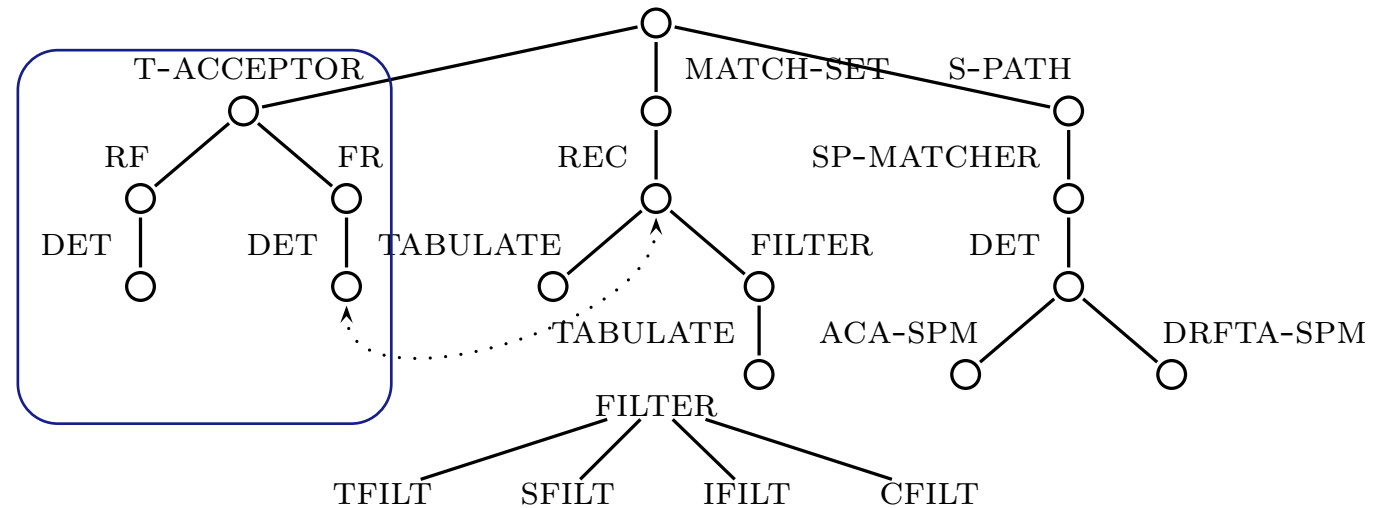
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## Overview - I



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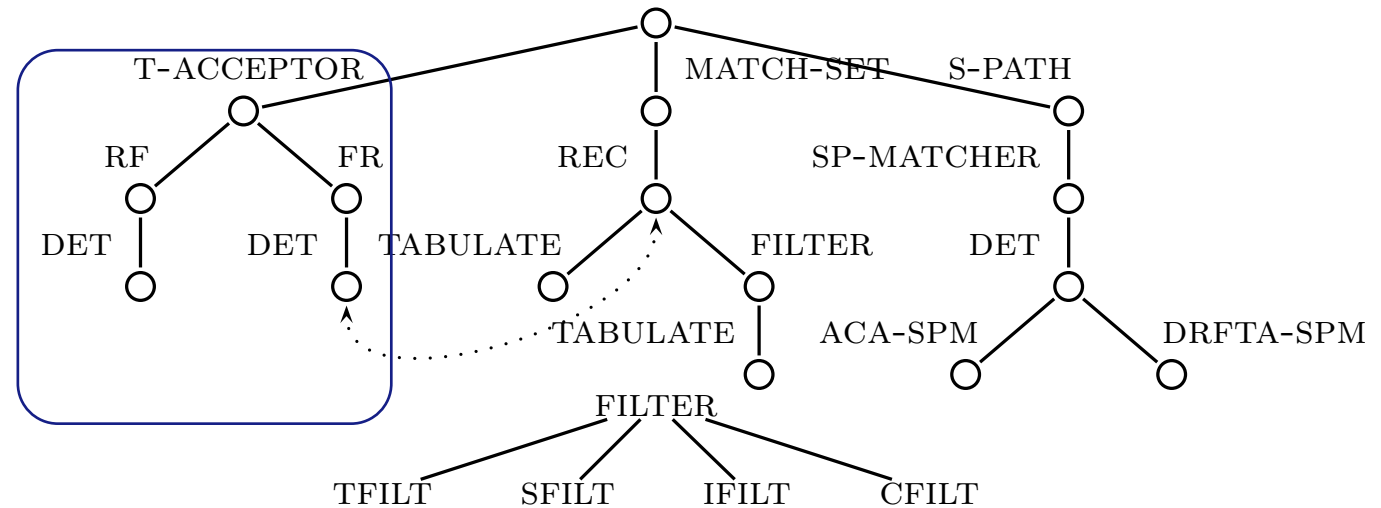
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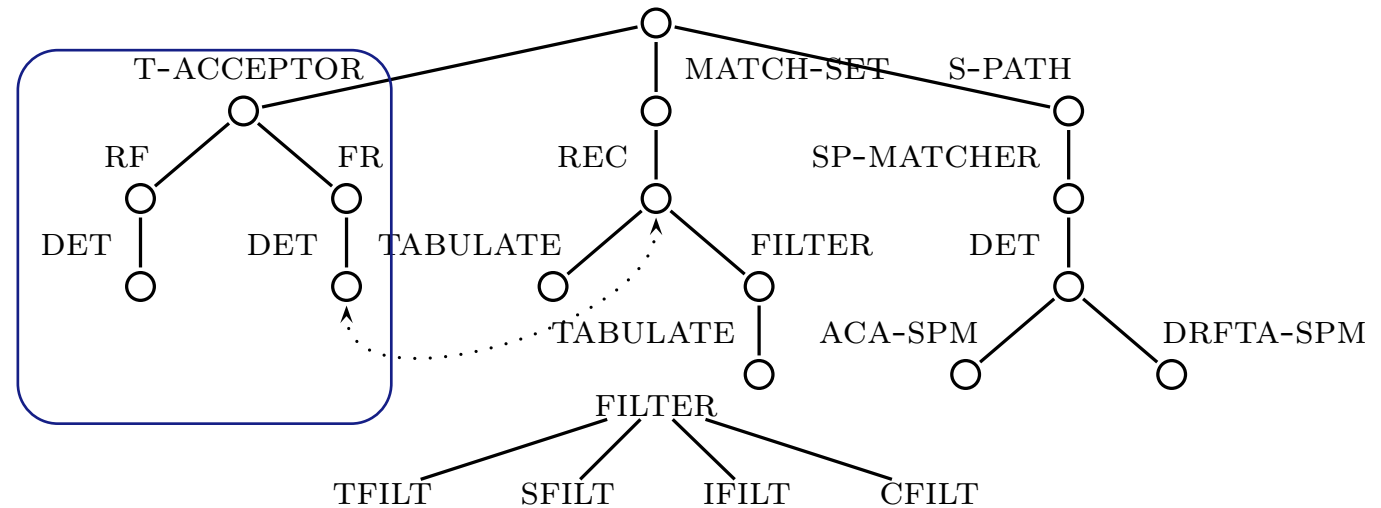
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- Algorithms based on correspondence between Regular Tree Grammars and Finite Tree Automata
  - For every RTG, undirected TA can be constructed
  - Adding details e.g. direction, determinacy, restricting grammar elements used for state set leads to other constructions

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## String Automata, Tree Automata

a b b

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- View automata as assigning states to positions ‘in between’ symbols

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|  
b  
|  
b  
|  
└

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 Note  $(q_3, ()) \in R_{\perp}$

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- For tree case, assigning states to positions of tree

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$q_0$   
a  
 $q_1$  |  
b  
 $q_2$  |  
b  
 $q_3$  |  
⊥

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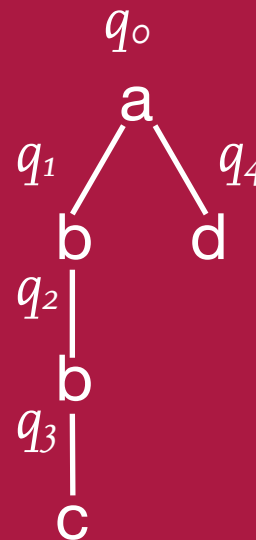
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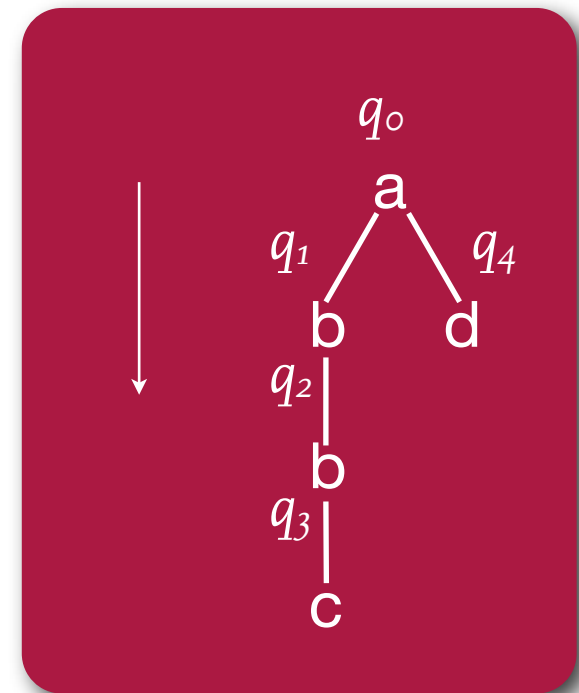
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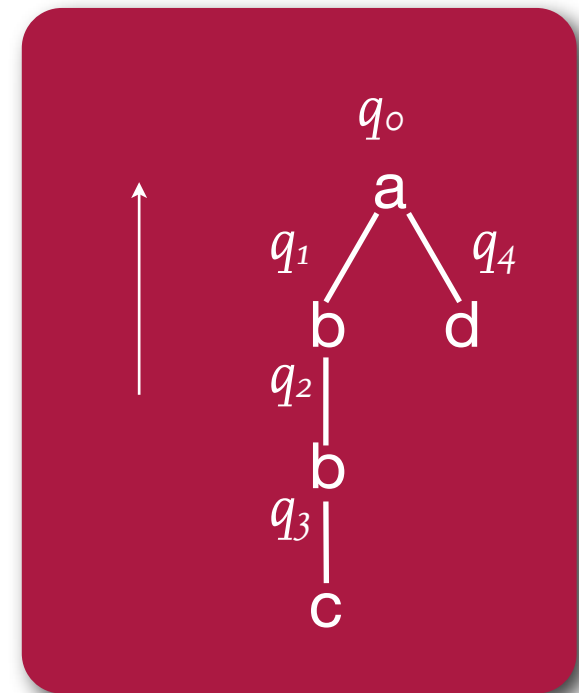
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- Direction
  - Top-Down (Root-to-Frontier)



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- Determinization
- For  $DFRTA$ , 4 types of *filtering* to reduce tables

# Tree Acceptance Taxonomy

## Tree Automata Constructions

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- About 50 different constructions in tree acceptance and tree pattern matching taxonomies



# Tree Acceptance Taxonomy

## Tree Automata Constructions

- About 50 different constructions in tree acceptance and tree pattern matching taxonomies
- Construction presentation
  - uniform style
  - defines state set, transition relation, ...
  - gives example
  - discusses correctness arguments
  - discusses related constructions and literature
  - identified by sequence of labels indicating details, e.g. (TGA-TA:ALL-SUB:REM-Epsilon:FR:SUBSET)

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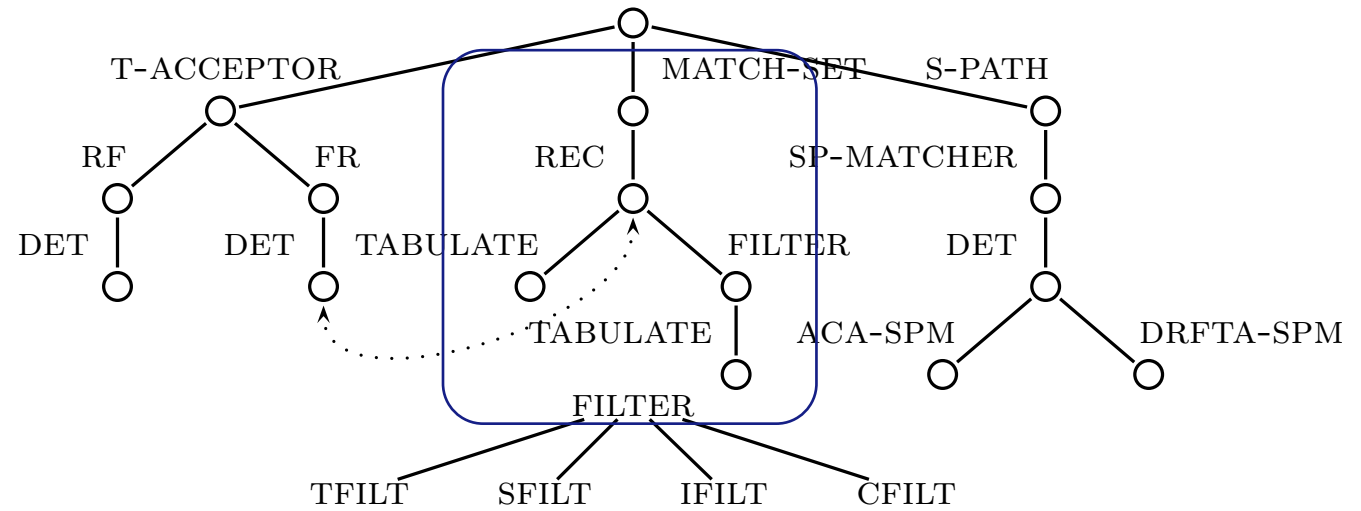
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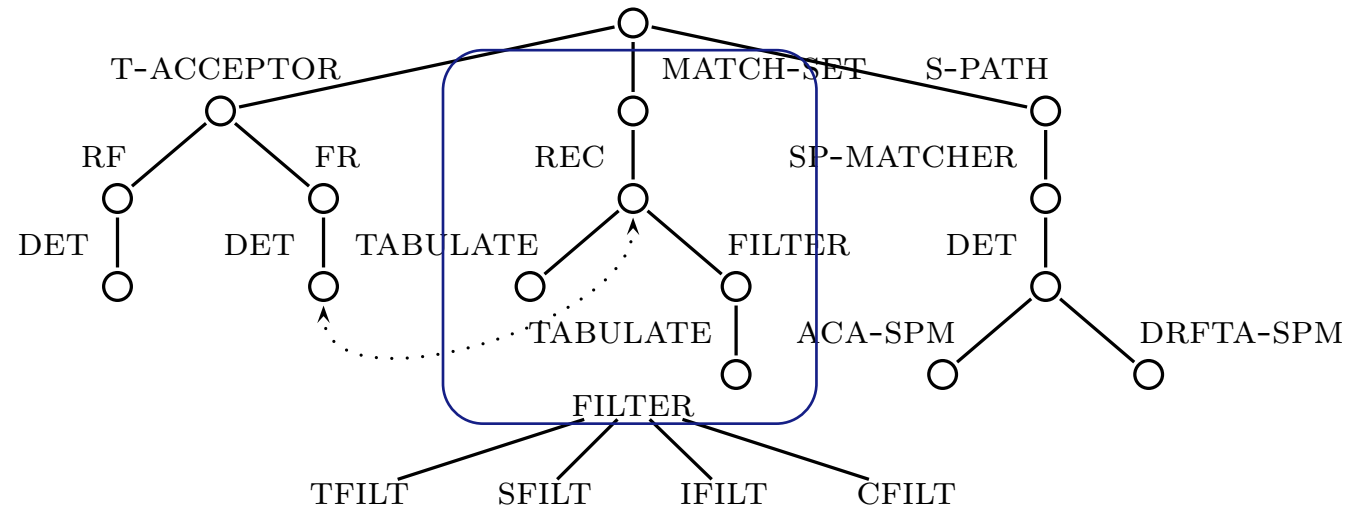
# Tree Acceptance Taxonomy

## Overview - II



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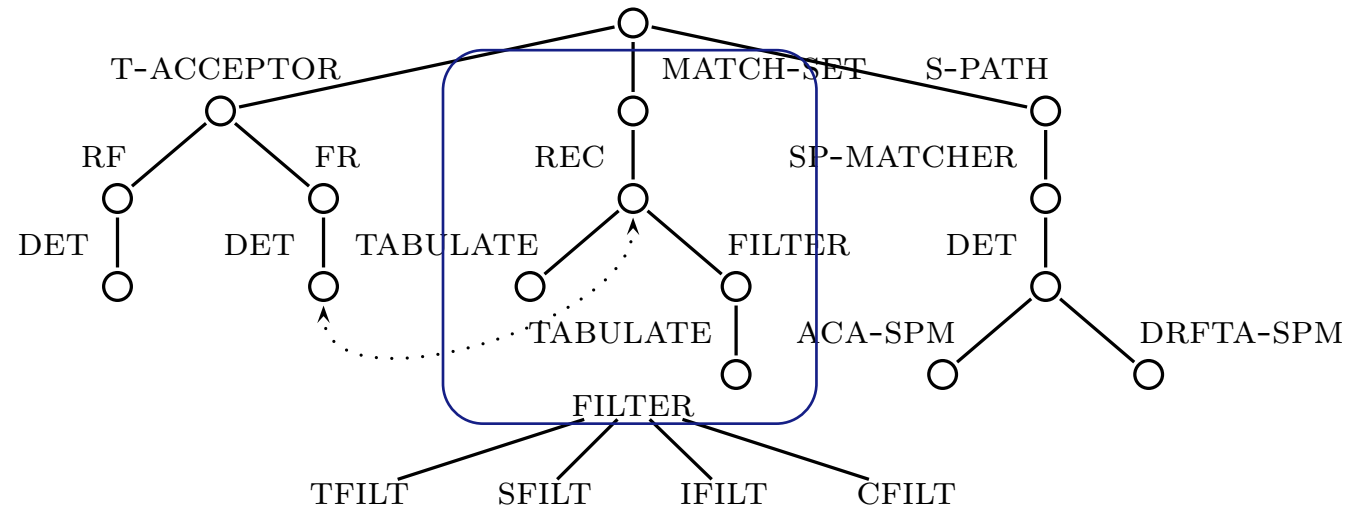
## Overview - II



- Algorithms based on suitable generalization of  $S \xRightarrow{*} t$

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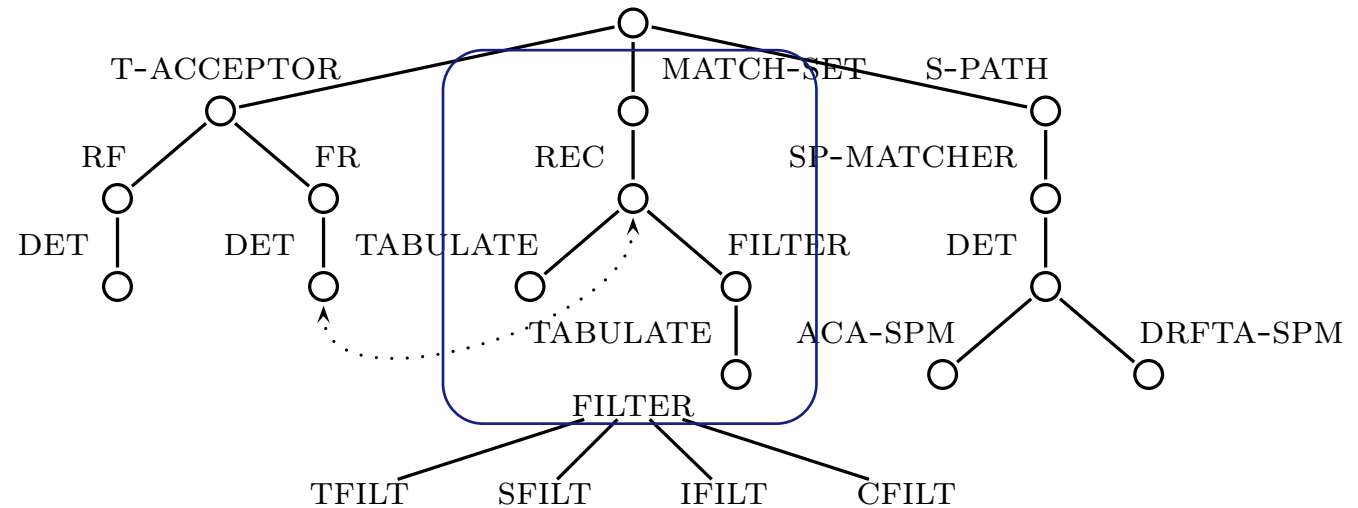
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- Algorithms based on suitable generalization of  $S \xRightarrow{*} t$ 
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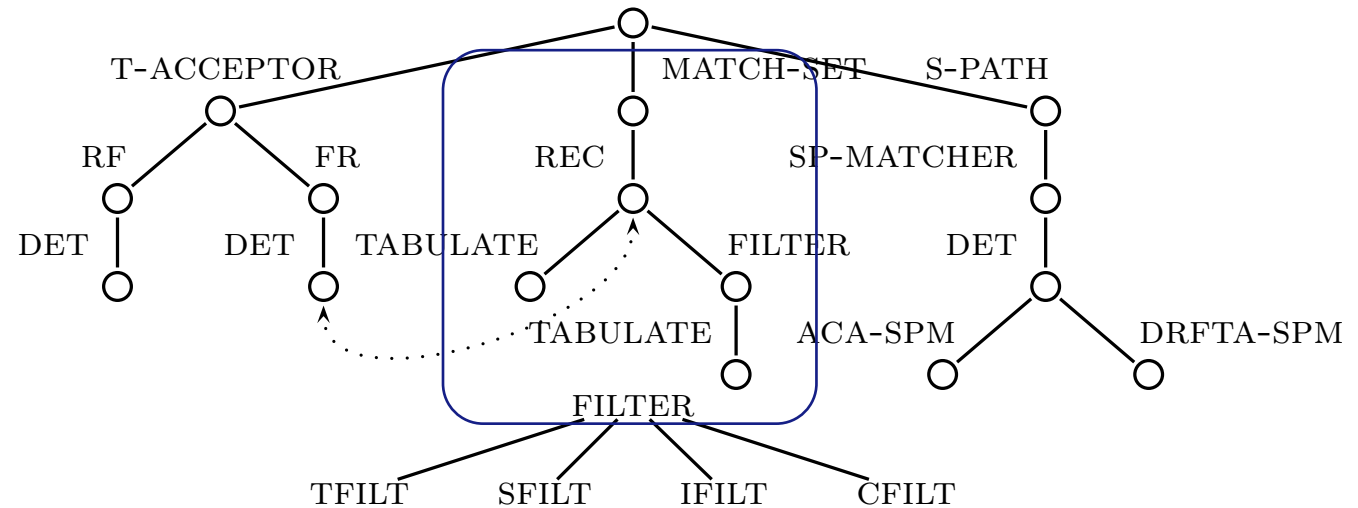
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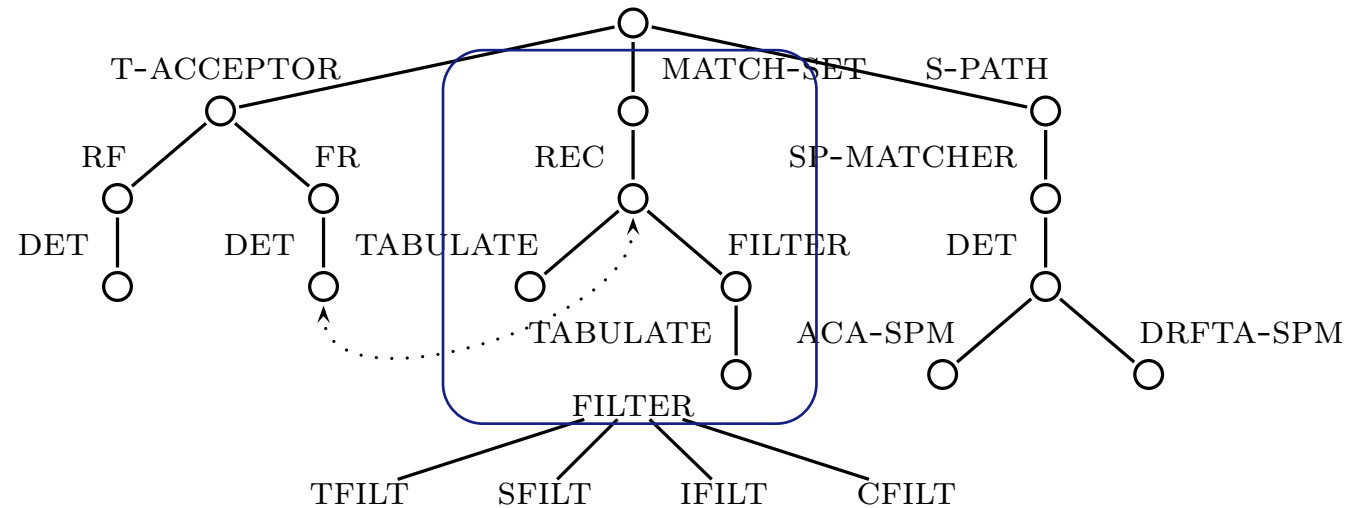
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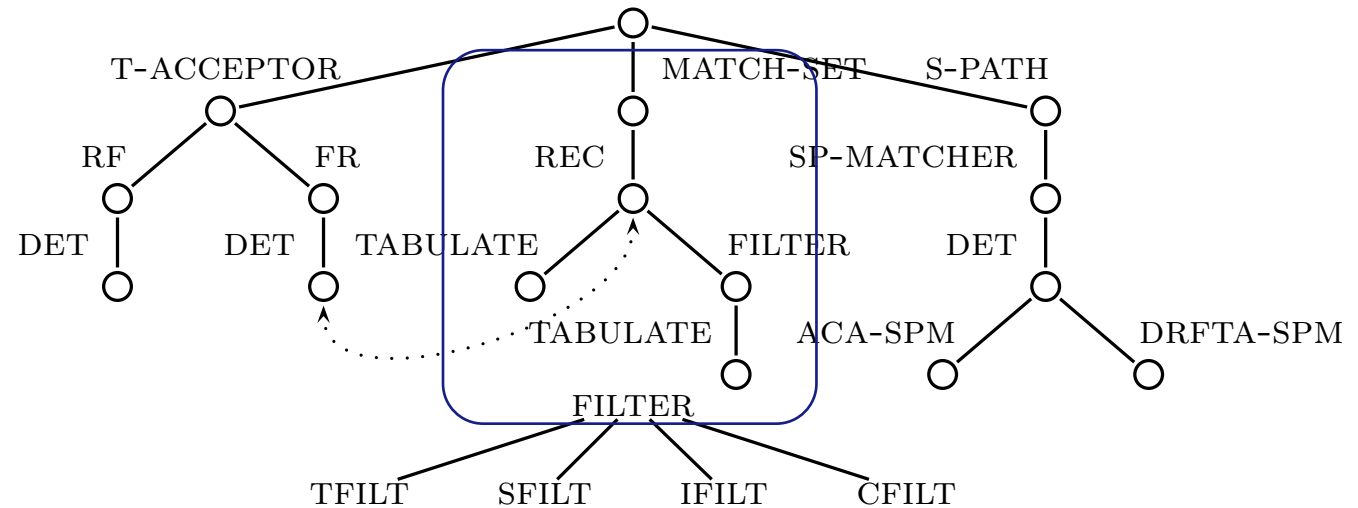
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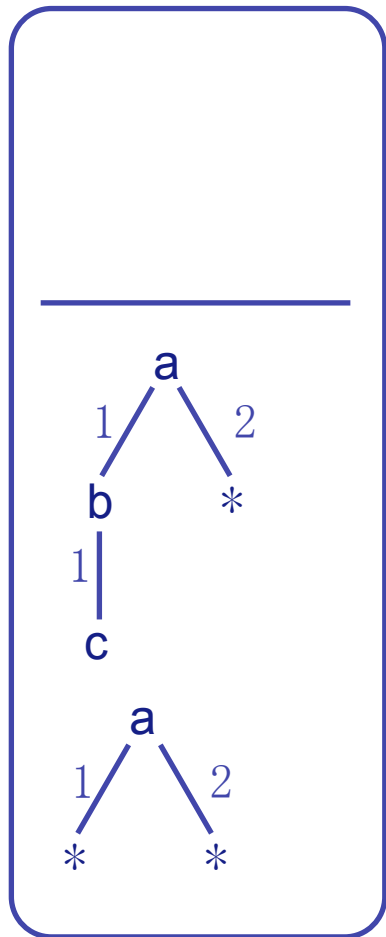


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  - Just a different view on *TAs*!



# Tree Acceptance Taxonomy

*Computing match sets; tree automata*



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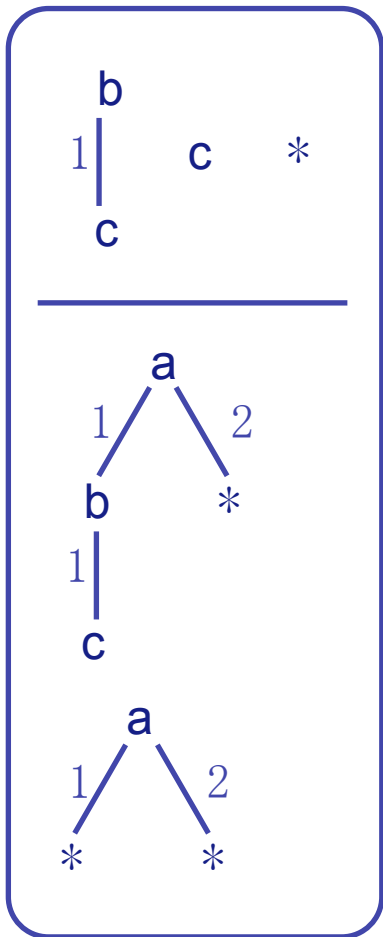


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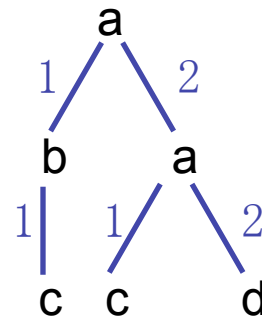
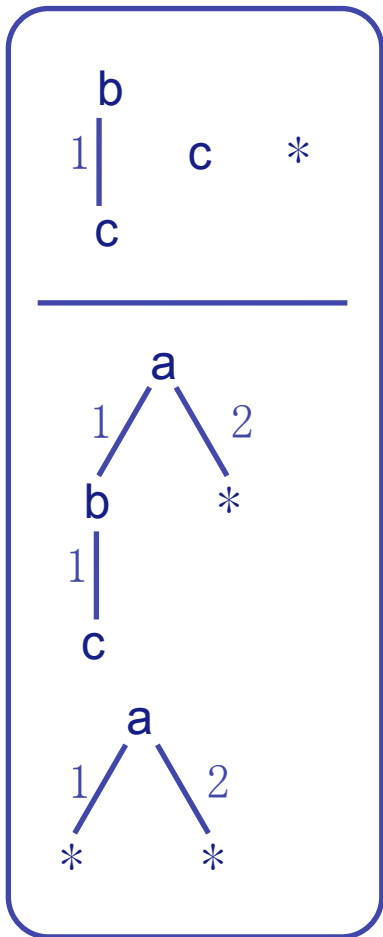
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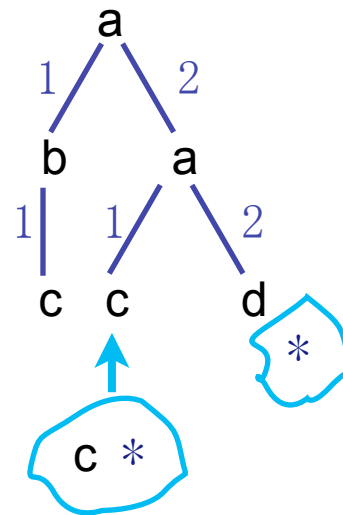
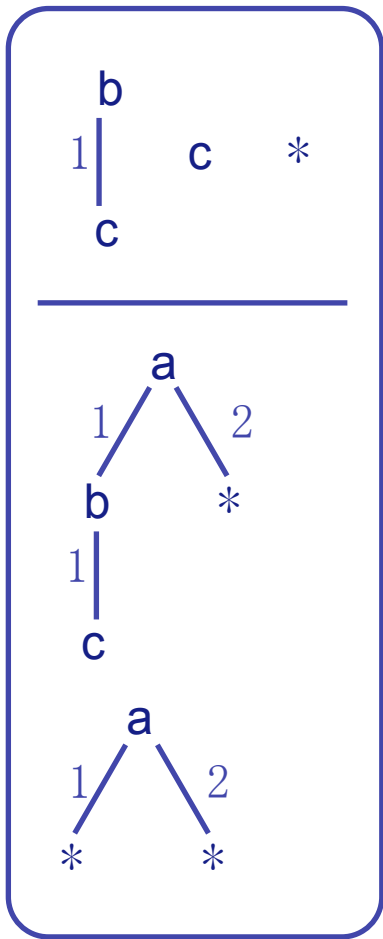
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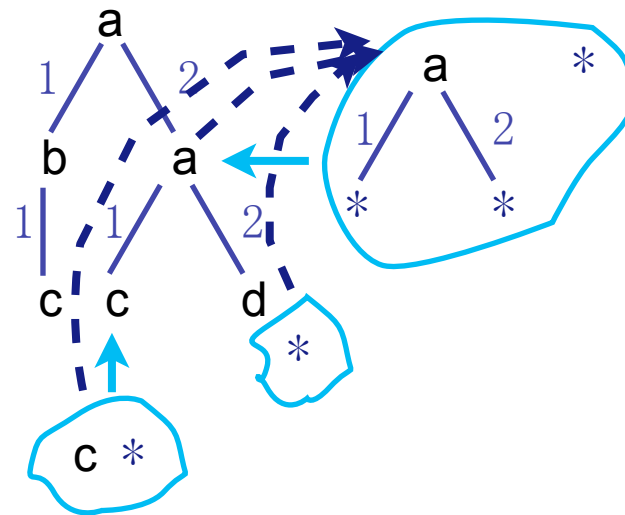
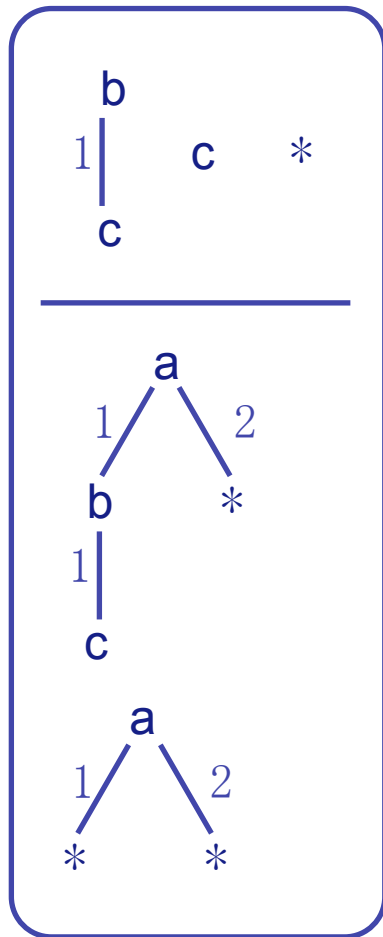
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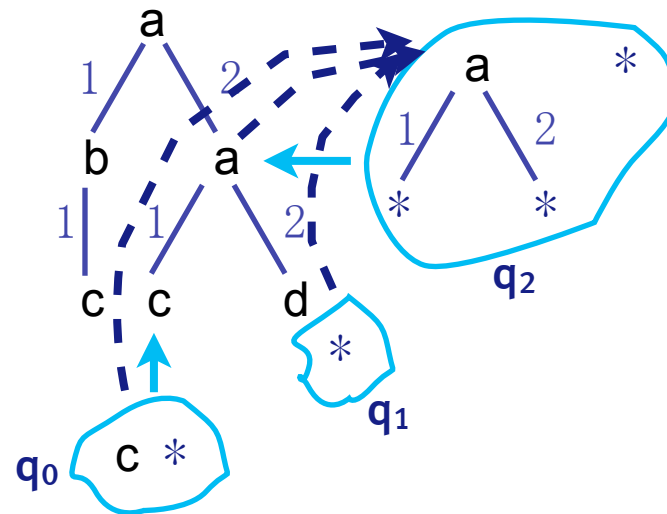
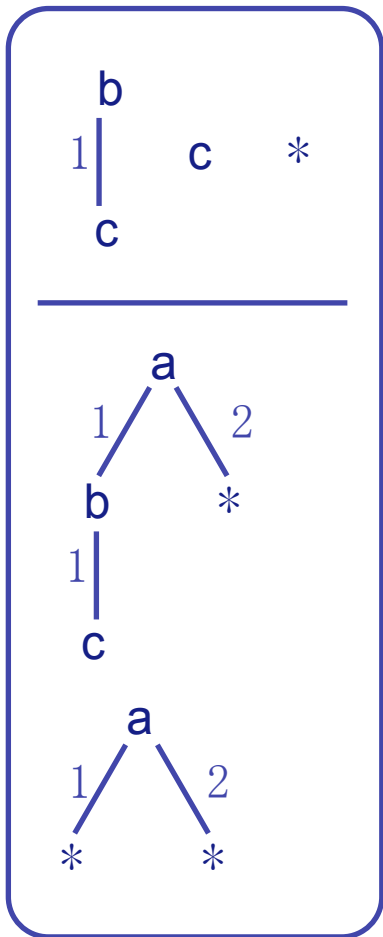
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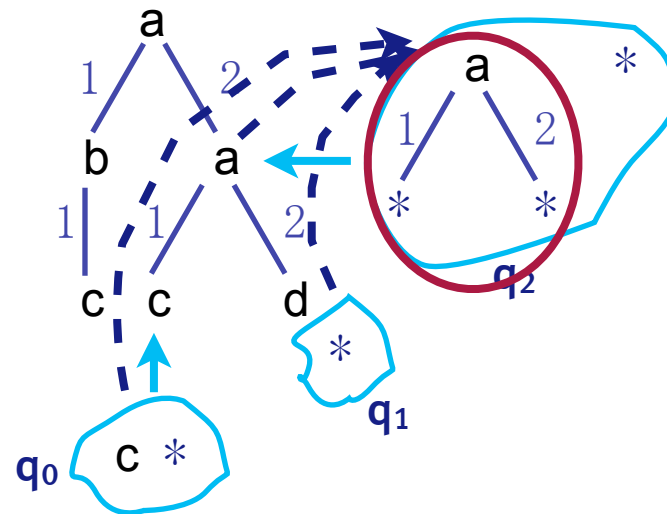
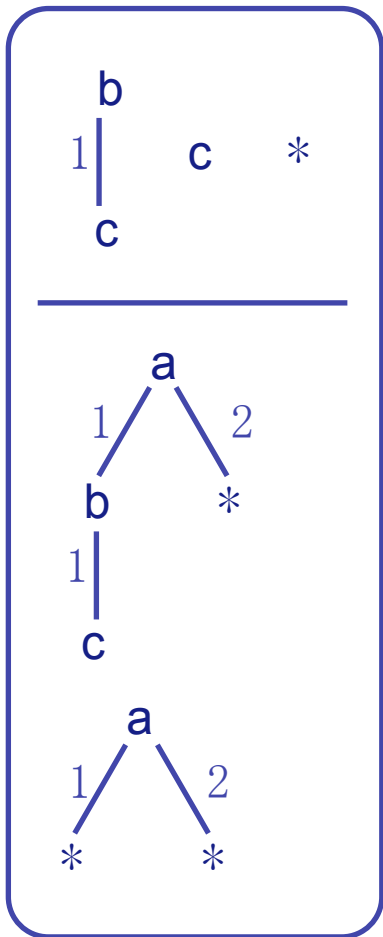
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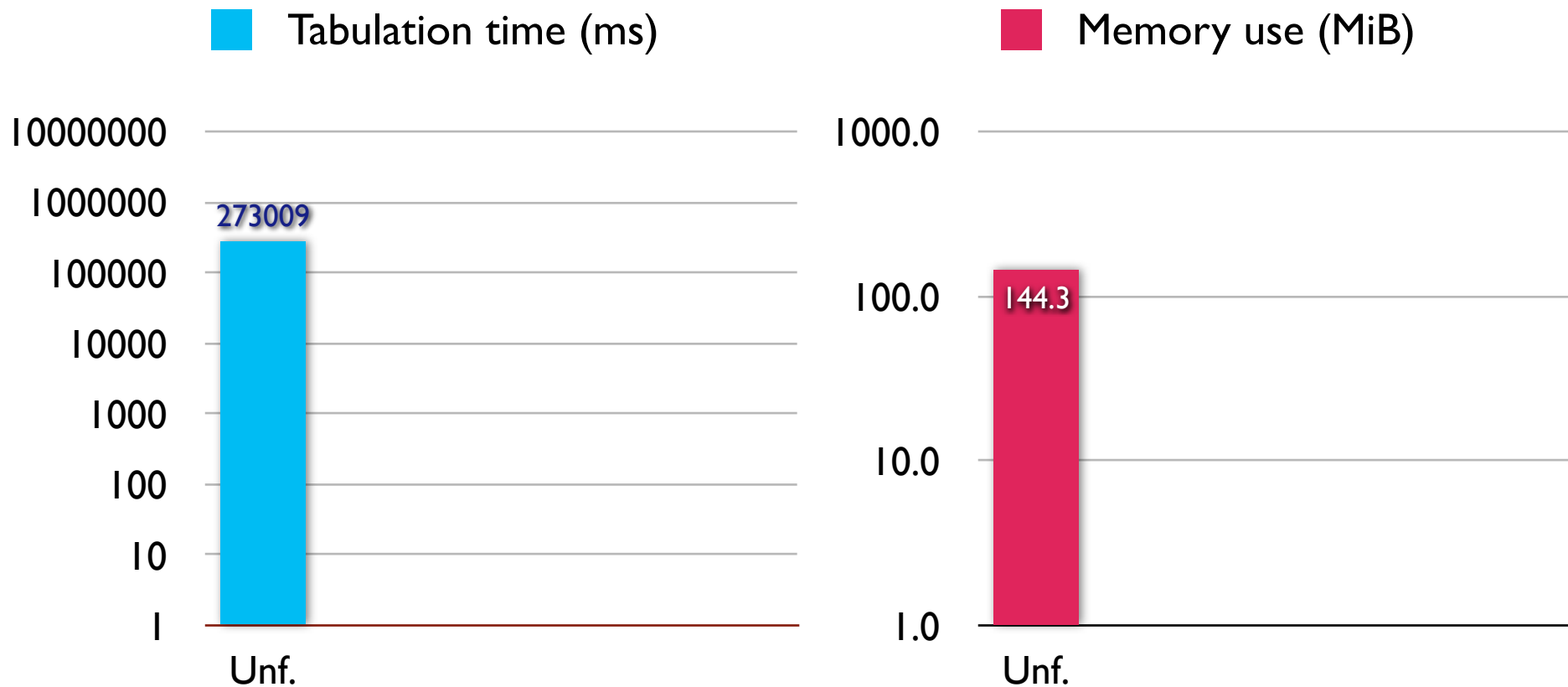
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# Tree Acceptance Taxonomy

## Practical Results - *Filtering match sets for instruction selection*

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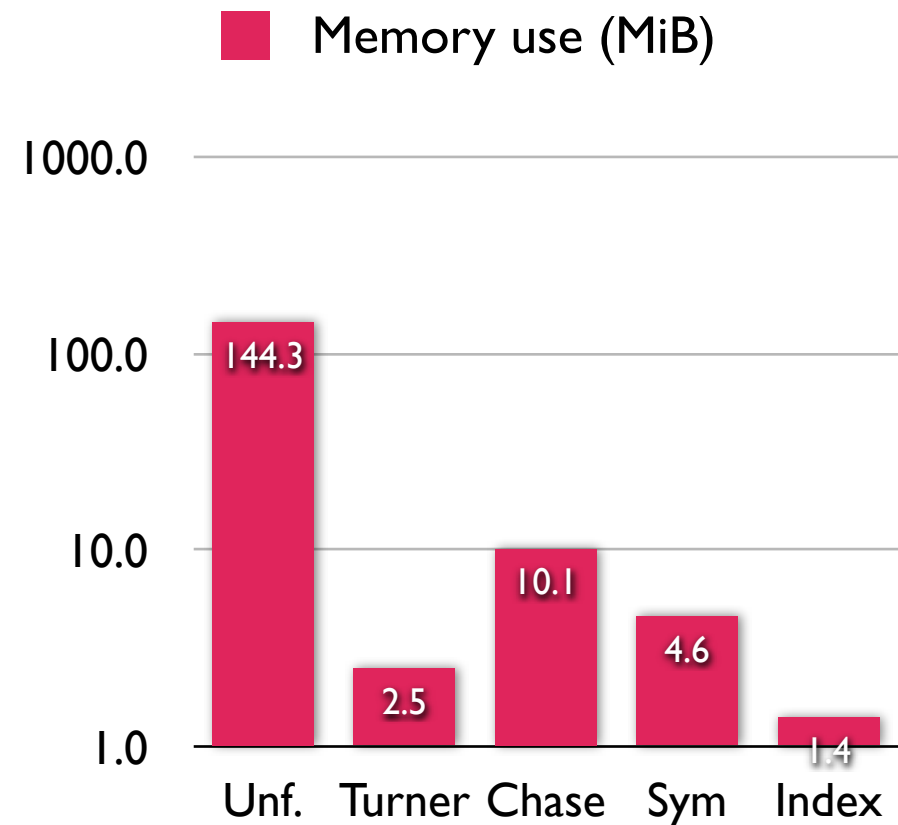
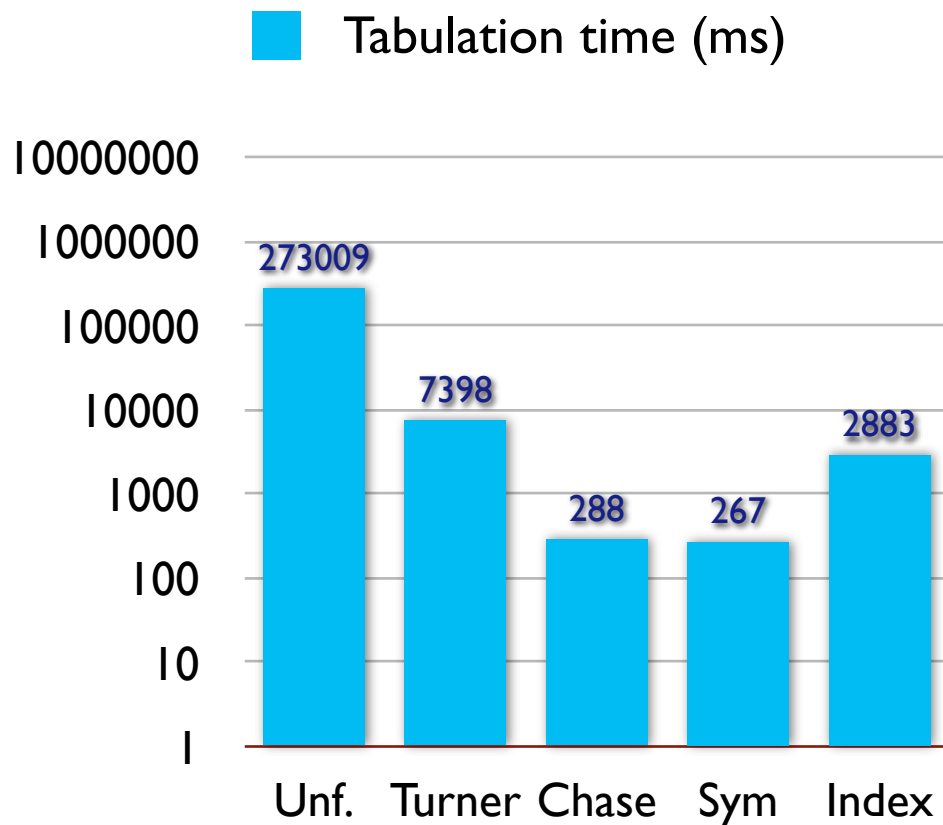




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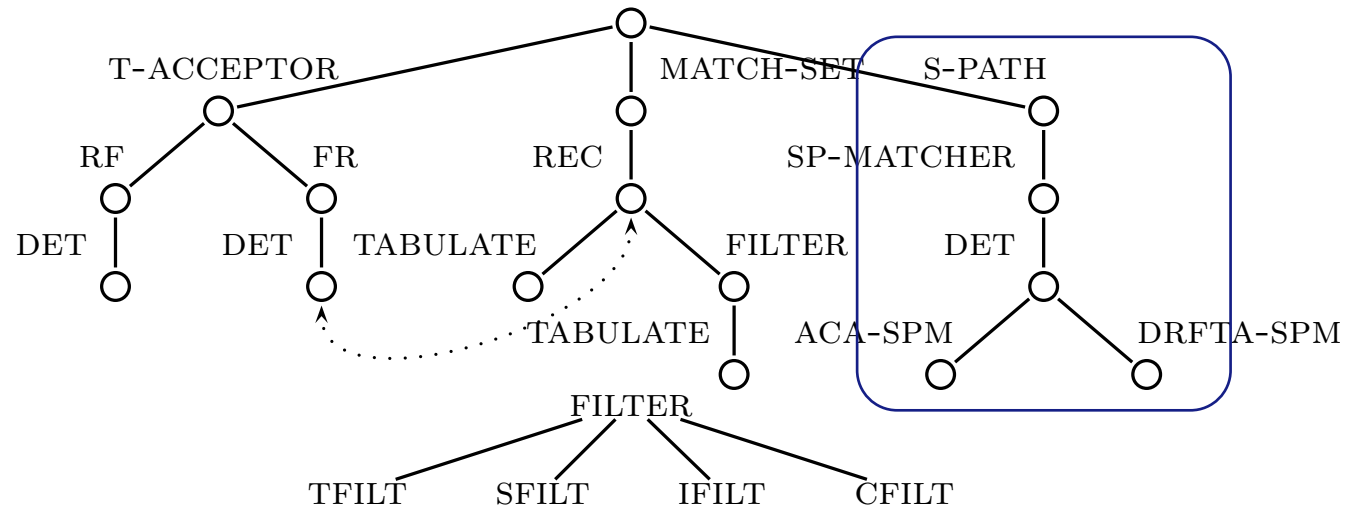
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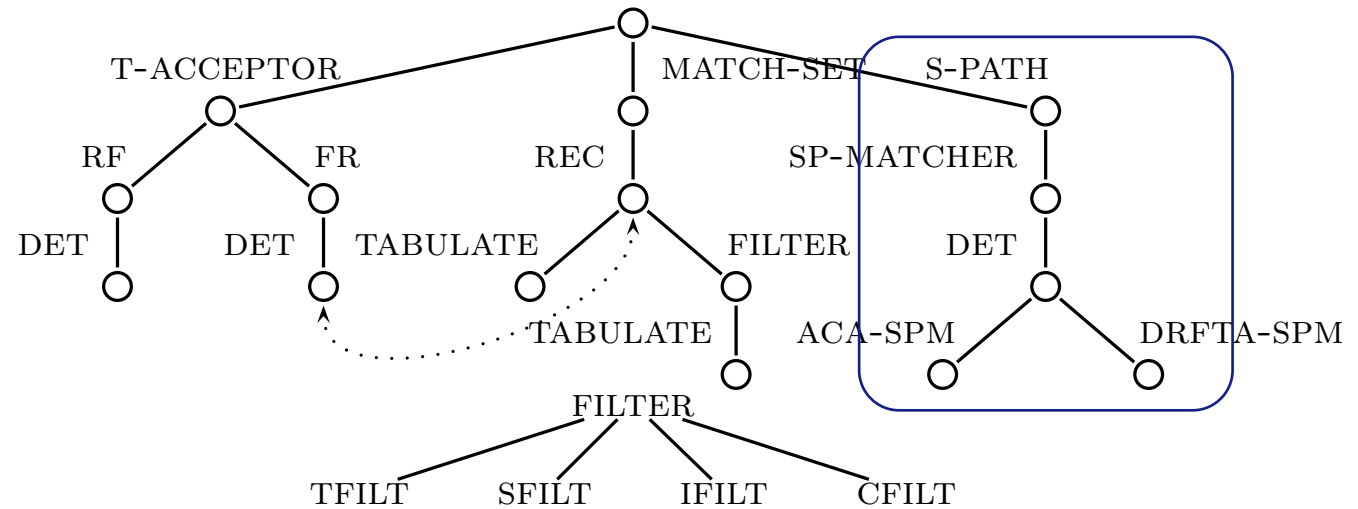
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## Overview - III



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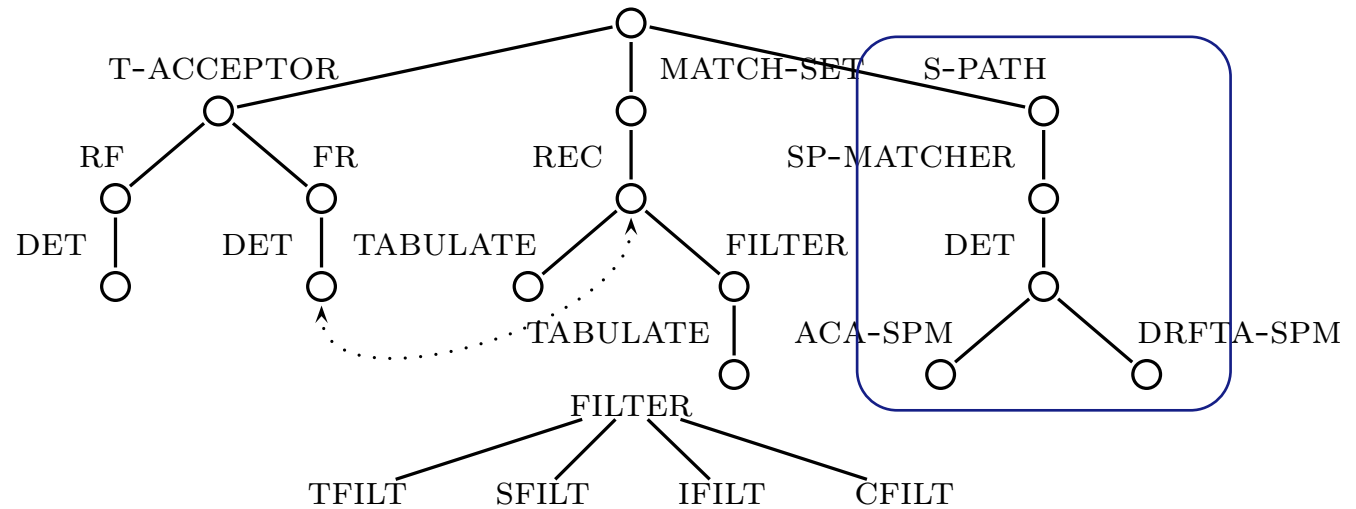
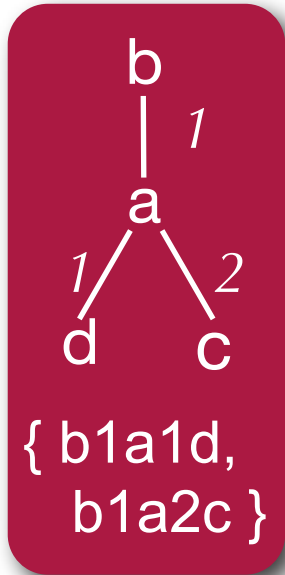
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- Algorithms based on decomposing items into stringpaths, use of string matching

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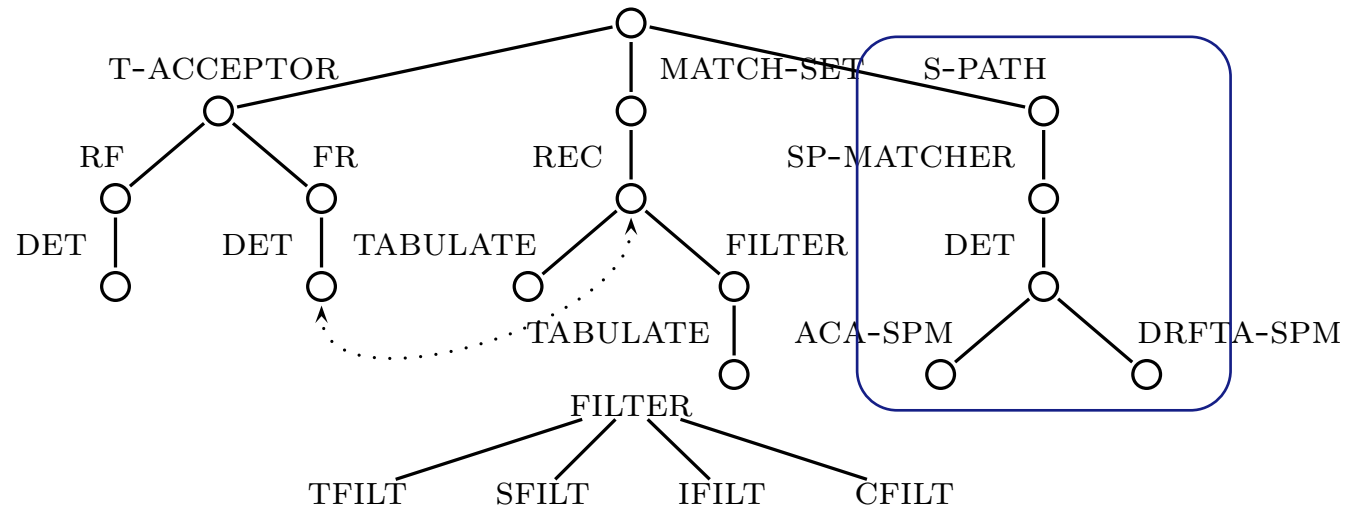
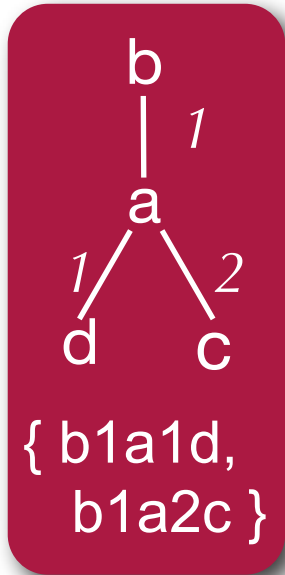
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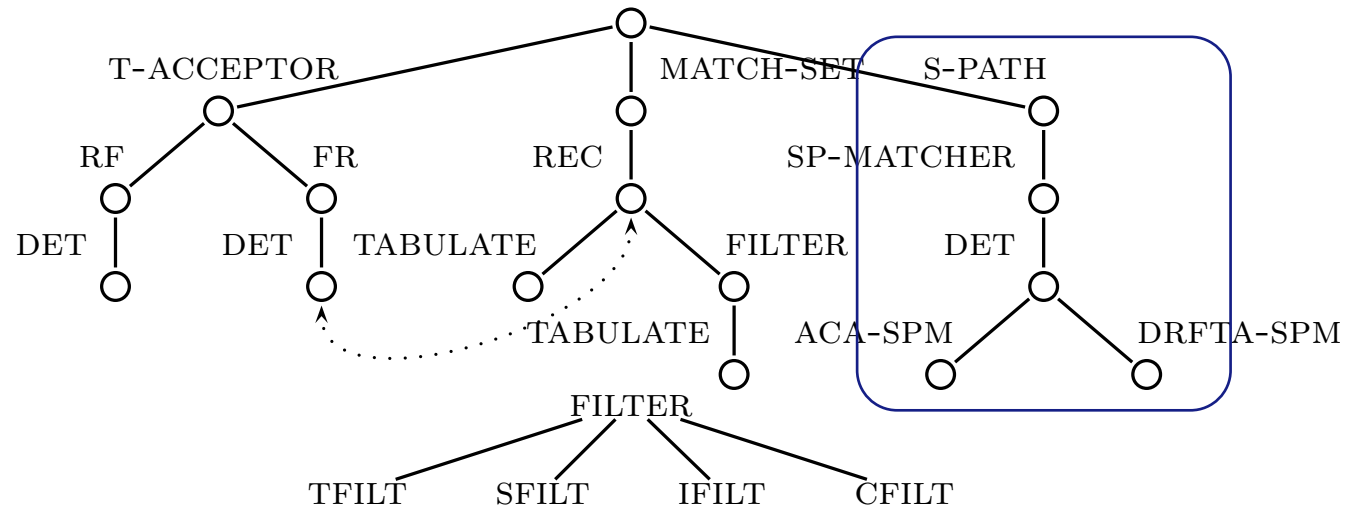
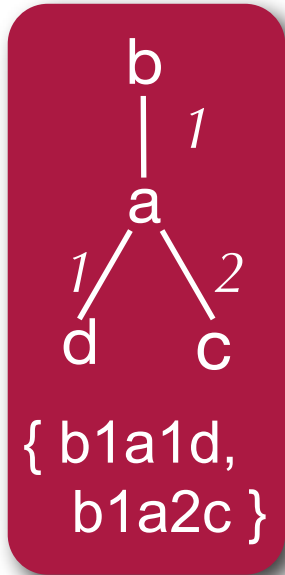
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- Algorithms based on decomposing items into stringpaths, use of string matching
  - Based on stringpath matches found, item matches and hence match sets can be computed for each subtree of  $t$
  - Different automata may be used for stringpath matching

- **Context**  
*History & relevance, deficiencies, role of taxonomies & toolkits*
- **Domain**  
*Trees, patterns & matching, regular tree grammars*
- **Taxonomies**  
*Algorithm taxonomies, taxonomies of regular tree algorithms*
- **Tree Acceptance Taxonomy**  
*Algorithms b/o tree automata, match sets, stringpath matching*
- **Concluding Remarks**

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- Lead to new/rediscovered algorithms/constructions
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- Implementation
  - *Forest FIRE* toolkit, *FIRE Wood* GUI; 138 interfaces/classes, ~16K LOC
  - *Java*, *SWT*, multi-platform
  - Available via <http://www.fastar.org>